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A. Appendix A: Transport Properties Correlations

A1: Pressure Drop

Friction factors from various scientists with their applicability range in terms of Reynolds number:

	Name	Equation	Reynolds Range
1	Ergun Equation	$f = \frac{1-\varepsilon}{\varepsilon^3} \left(1.75 + 150 \frac{1-\varepsilon}{Re'} \right)$	$Re/(1-\varepsilon) < 500$
2	Handley & Heggs	$f = \frac{1-\varepsilon}{\varepsilon^3} \left(1.24 + 368 \frac{1-\varepsilon}{Re'} \right)$	$1000 < Re/(1-\varepsilon) < 5000$
3	Hicks	$f = 6.8 \frac{(1-\varepsilon)^{1.2}}{\varepsilon^3} Re^{-0.2}$	
4	Leva	$\frac{dp_t}{dz} + 200G \frac{\mu(1-\varepsilon)^2}{d_p^2 \psi^2 \rho_g g \varepsilon^3} = 0$ $\frac{dp_t}{dz} + 3.5 \frac{G^{1.9} \mu^{0.1} (1-\varepsilon)^{1.1}}{d_p^{1.1} \psi^{1.1} \rho_g g \varepsilon^3} = 0$	Laminar Turbulent
5	Leva	$\frac{dp_t}{dz} + \frac{2 f_m G^2 (1-\varepsilon)^{3-n}}{d_p \psi^{3-n} \rho_g g \varepsilon^3} = 0$	Laminar and Turbulent

Carman-Kozeny Permeability (Baker, 2011):

$$K_{pb} = \frac{\varepsilon^3}{180(1-\varepsilon)^2} d_p^2 \quad [64]$$

Appendix A: Transport Properties Correlations

A1.2 Particle Reynolds number (Baker, 2011):

$$\text{Re}_{d_p} = \frac{u \rho d_p}{\mu(1-\varepsilon)} \quad [65]$$

A1.3 Particle Volume equivalent diameter (Baker, 2011):

$$d_p = \frac{6(1-\varepsilon)}{a_p} \quad [66]$$

Where:

- a_p is the specific surface area, $\frac{S_p}{V_p}$
- S_p is the particle surface area
- V_p is the particle volume

A2: Heat Transfer Correlations

A2.1: Thermal conductivity in packed bed

Levas correlation (Brecher, 1977)

$$\frac{\alpha_i d_t}{\lambda_g} = 0.813 \left(\frac{d_p G}{\mu} \right)^{0.9} e^{-6d_p/d_t} \quad [67]$$

A2.2: Radial Effective thermal conductivity

A2.2.1 Bauer & Schlünder (Bauer, 1978)

$$\frac{\lambda_{\text{convection}}}{\lambda_f} = \frac{\rho u c_p}{\lambda_f} \frac{X_F}{8 \left[2 - \left(1 - 2 d_{pv}/d_t \right)^2 \right]} \quad [68]$$

$X_F = F d_{pv}$ with $F=1.75$ for cylindrical particles

$$\frac{\lambda_{\text{conduction,radiation}}}{\lambda_f} = (1 - \sqrt{1 - \varepsilon}) \left(1 + \varepsilon \frac{\lambda_{\text{radiation}}}{\lambda_f} \right) + \sqrt{1 - \varepsilon} \left(\frac{\lambda_{rs}}{\lambda_f} \right)$$

$$\frac{\lambda_{\text{radiation}}}{\lambda_f} = 2.27 \cdot 10^{-7} \frac{e}{2 - e} T^3 \frac{d_{pv}}{\lambda_f}$$

$$\frac{\lambda_{rs}}{\lambda_f} = \frac{2}{N} \left[\frac{B(k_s + k_r - 1)}{N^2 k_s} \ln \left(\frac{k_s + k_r}{B} \right) + \frac{B+1}{2B} (k_r - B) - \frac{B-1}{N} \right]$$

$$N = \frac{k_s + k_r - B}{k_s}$$

$$B = C \left(\frac{1 - \varepsilon}{\varepsilon} \right)^{10/9}$$

$$k_s = \frac{\lambda_{\text{solid}}}{\lambda_f}$$

$$k_r = \frac{\lambda_{\text{radiation}}}{\lambda_f}$$

X_F is effective mixing length, $X_F = F d_{pv}$

F=1.75 for cylindrical particles

C=2.5 for cylindrical particles

A2.2.2 Dixon (Dixon, 1979)

$$\frac{1}{Pe_{er}} = \frac{1}{Pe_{fr}} + \frac{\lambda_{rs}/\lambda_f}{Re Pr} \left[\frac{Bi_f + 4}{Bi_f} \right] \left[\frac{8}{N_s} + \frac{Bi_s + 4}{Bi_s} \right]^{-1} \quad [69]$$

(Re>50)

$$\frac{1}{Pe_{er}} = \frac{1}{Pe_{fr}} \left[\frac{Bi_s + 4}{Bi_s} \right] \left[\frac{8}{N_F} + \frac{Bi_f + 4}{Bi_f} \right]^{-1} + \frac{\lambda_{rs}/\lambda_f}{Re Pr} \quad (Re < 50)$$

Appendix A: Transport Properties Correlations

$$\frac{1}{Pe_{rf}} = \frac{1}{Pe_{rf}(\infty)} + \frac{0.74\varepsilon}{Re Pr}$$

$$Pe_{rf}(\infty) = 7 \quad \text{for cylindrical particles}$$

$$\frac{\lambda_{rs}}{\lambda_f} = \sqrt{1-\varepsilon} \frac{2}{M} \left[\frac{B(k_s-1)}{M^2 k_s} \ln\left(\frac{k_s}{B}\right) - \frac{B+1}{2} - \frac{B-1}{M} \right]$$

$$M = \frac{k_s - B}{k_s} \quad k_s = \frac{\lambda_{solid}}{\lambda_f} \quad B = C \left(\frac{1-\varepsilon}{\varepsilon} \right)^{10/9}$$

$$Bi_f = Nu_{wf} \left(d_t / 2d_{pv} \right) (Pe_{rf} / (Re Pr))$$

$$Nu_{fs} = 2.0 + 1.1 Pr^{1/3} Re^{0.6}$$

$$Nu_{wf} = 0.523 (1 - d_{pv} / d_t) Pr^{0.33} Re^{0.738}$$

$$Bi_s = 0.48 + 0.192 \left(d_t / d_{pv} - 1 \right)^2 \quad \text{for cylinders}$$

$$\beta_s = \frac{\lambda_{rs} / \lambda_f}{\frac{8}{N_s} + \frac{Bi_s + 4}{Bi_s}} \quad \beta_f = \frac{Re Pr / Pe_{rf}}{\frac{8}{N_s} + \frac{Bi_f + 4}{Bi_f}} \quad N_s = \frac{0.25(1-\varepsilon) \frac{A_p}{V_p} \frac{d_t^2}{d_{pv}}}{\frac{\lambda_{rs}}{\lambda_f} \left[\frac{1}{Nu_{fs}} + \frac{1}{\beta} \frac{\lambda_f}{\lambda_{solid}} \right]}$$

$$N_F = \frac{0.25(1-\varepsilon) \frac{A_p}{V_p} \frac{d_t^2}{d_{pv}}}{\frac{Re Pr}{Pe_{rf}} \left[\frac{1}{Nu_{fs}} + \frac{1}{\beta} \frac{\lambda_f}{\lambda_{solid}} \right]} \quad \beta = 8 \quad C = 2.5 \quad \text{for cylindrical particles}$$

A2.3: Wall heat transfer coefficient

A2.3.1 Dixon (1988)

$$Nu_w = \frac{h_w d_{pv}}{\lambda_f} = \frac{8\beta_s}{d_t / d_{pv}} + Nu_{wf} \left(1 + \beta_s \frac{Pe_{rf}}{Re_{pv} Pr} \right)$$

[70]

$$Re > 50$$

$$Nu_w = \frac{h_w d_{pv}}{\lambda_f} = \frac{8\beta_s}{d_t/d_{pv}} + 2Bi_s \frac{\lambda_{rs}}{\lambda_f} \frac{d_{pv}}{d_t} \left(1 + \frac{\beta_f}{\lambda_{rs}/\lambda_f} \right) \quad \text{Re} < 50$$

The definitions for β_s , β_f , λ_{rs} , Bi_s , Pe_{rf} are given in (Dixon 2 by effective radial conductivity)

A2.3.2 Li & Finlayson (1977)

For cylindrical particles, $20 < Re_h < 800$, $0.03 < d_h/d_t < 0.2$

$$Nu_w = \frac{h_w d_{pv}}{\lambda_f} = 0.18 Re_h^{0.93} Pr^{0.33} \frac{d_{pv}}{d_h} \quad [71]$$

A2.4: Overall heat transfer coefficient

A2.4.1 Dixon (1988)

$$\frac{1}{U_w} = \frac{1}{h_w} + \frac{d_t}{6\lambda_{er}} \frac{Bi + 3}{Bi + 4} \quad [72]$$

$$Nu_{fw} = 0.523 \left(1 - \frac{d_{pv}}{d_t} \right) Pr^{0.33} Re_{pv}^{0.738}$$

$$Nu_w = \frac{h_w d_{pv}}{\lambda_f} = \frac{8\beta_s}{d_t/d_{pv}} + Nu_{wf} \left(1 + \beta_s \frac{Pe_{rf}}{Re_{pv} Pr} \right) \quad \text{Re} > 50$$

$$Nu_w = \frac{h_w d_{pv}}{\lambda_f} = \frac{8\beta_s}{d_t/d_{pv}} + 2Bi_s \frac{\lambda_{rs}}{\lambda_f} \frac{d_{pv}}{d_t} \left(1 + \frac{\beta_f}{\lambda_{rs}/\lambda_f} \right) \quad \text{Re} < 50$$

$$Bi = \frac{d_t}{2d_{pv}} \frac{Nu_w Pe_{er}}{Re_{pv} Pr}$$

The definitions for β_s , β_f , λ_{rs} , Bi_s , Pe_{rf} are given in (Dixon 2 by effective radial conductivity)

A2.4.2 Li & Finlayson (1977)

Appendix A: Transport Properties Correlations

For cylindrical particles, $20 < \text{Re}_h < 800, 0.03 < d_h/d_t < 0.2$

$$\frac{U_w d_t}{\lambda_f} = 1.40 \text{Re}_h^{0.95} \text{Pr}^{0.33} \exp\left(-\frac{6d_h}{d_t}\right) \quad [73]$$

A2.5 Effective radial diffusivity (D_{er})

A2.5.1 Bauer and Schlünder (1978)

$$D_{er} = \frac{uX_F}{8 \left[2 - \left(1 - 2d_{pv}/d_t \right)^2 \right]} \quad [74]$$

$$X_F = Fd_{pv}$$

F=1.75 for cylindrical particles

A2.5.2 Rase (1990)

$$\text{For } d_{pa}/d_t > 0.1 \text{ use } \frac{\varepsilon D_{er}}{ud_{pa}} = \frac{1}{m} + \frac{0.38}{\text{Re}} \quad [75]$$

$$\text{For } d_{pa}/d_t < 0.1 \text{ divide } D_{er} \text{ calculated above by } \left[1 + 19.4 \left(\frac{d_{pa}}{d_t} \right)^2 \right]$$

$$m = \begin{cases} 11 & \text{Re} > 400 \\ 57.85 - 35.36 \log \text{Re} + 6.68 (\log \text{Re})^2 & 20 < \text{Re} < 400 \end{cases}$$

A2.5.3 Specchia et al. (1980)

$$D_{er} = \frac{ud_{pa}}{8.65 \left[1 + 19.4 \left(\frac{d_{pd}}{d_t} \right)^2 \right]} \quad [76]$$

A2.6 Solid-Fluid heat and mass transfer coefficient

A2.6.1 Gnielinski (1982) & Martin (1978)

$$Nu_{particle} = 2 + F Re_c^{0.5} Pr^{0.33} \quad [77]$$

$$Re_{pa} = u_f \rho_f d_{pa} / (\varepsilon \mu_f) \quad Pr = \frac{C_p \mu_f}{\lambda_f}$$

$$F = 0.664 \sqrt{\left[1 + \left(\frac{0.0557 Re_c^{0.3} Pr^{0.67}}{1 + 2.44 (Pr^{0.67} - 1) Re_c^{-0.1}} \right)^2 \right]}$$

$$Nu = [1 + 1.5(1 - \varepsilon)] Nu_{particle} \frac{d_{pv}}{d_c}$$

$$0.26 < \varepsilon < 0.935$$

$$0.6 < Pr < 10000$$

$$Re_p Pr > 100$$

A2.5.3 Bird et al. (1960)

$$Nu = 2.27 (1 - \varepsilon)^{0.51} \psi^{1.51} Re_h^{0.49} Pr^{0.33} \frac{d_{pv}}{d_h} \quad [78]$$

$$Re_h / (1 - \varepsilon) < 300$$

$$Nu = 1.27 (1 - \varepsilon)^{0.41} \psi^{1.41} Re_h^{0.59} Pr^{0.33} \frac{d_{pv}}{d_h} \quad Re_h / (1 - \varepsilon) > 300$$

$$\psi = 0.91 \text{ for cylindrical particles}$$

$$Re_h = \frac{u_f \rho_f d_h}{\mu_f} \quad Pr = \frac{C_p \mu_f}{\lambda_f} \quad Nu = \frac{\alpha_s d_{pv}}{\lambda_f}$$

A2.5.4 Chilton-Colburn analogy (Westertep, 1984)

$$Nu = Sh \left(\frac{Pr}{Sc} \right)^{\frac{1}{3}} \quad [79]$$

Wilke & Hougen (Berty, 1999)

$$j_h = 1.95 \text{Re}_p^{-0.51}$$

$$j_d = 1.82 \text{Re}_p^{-0.51}$$

Where:

$$\text{Re}_p = Gd_p / \mu \quad \text{for } \text{Re}_p < 350$$

With:

$$j_h \equiv St \text{Pr}^{0.66}$$

$$j_d \equiv St' Sc^{0.66}$$

A2.5.5 Heat Peclet number

To describe the dimensionless effective radial thermal conductivity to following can be applied (Koning, 2002):

$$\frac{\lambda_{e,r}}{\lambda_f} = \frac{\lambda_r^0}{\lambda_f} + \frac{Pe_h^0}{Pe_{h,r}^\infty} \quad [80]$$

Where:

➤ Molecular Peclet number: $Pe_h^0 = \frac{u_0 \rho_f C_{p,f} d_p^v}{\lambda_f}$

➤ Peclet number dependant on the aspect ratio: $Pe_{h,r}^\infty = 8 \left[2 - \left(1 - \frac{2}{N} \right)^2 \right]$

➤ Aspect ratio: $N = \frac{D_t}{d_p^v}$

A2.5.6 Mass Peclet number (Fahien, 1955)

Radial mass transfer for packings of different shapes.

$$Pe_{m,r}^{\infty} = C \left[1 + \frac{19.4}{N^2} \right] \quad [81]$$

Where:

$$\text{➤ } C = 8.65 \frac{d_p^v}{d_p^a}$$

$$\text{➤ } \text{Aspect ratio: } N = \frac{D_t}{d_p^a}$$

➤ Volume equivalent diameter of sphere with same diameter as surface area of particles in the

$$\text{packing } d_p^a = d \sqrt{\frac{1}{2} + \frac{h}{d}}$$

A2.7 Axial dispersion of heat and mass

A2.7.1 Edwards & Richardson (1968)

Mass dispersion

$$\frac{1}{Pe_{mz}} = \frac{0.73\varepsilon}{Re Sc} + \frac{0.5}{\left(1 + \frac{9.7\varepsilon}{Re Sc}\right)} \quad [82]$$

$$0.008 < Re < 50, 0.0377 < d_p < 0.6 \text{ cm}$$

A2.7.2 Wen & Fan (1975)

$$\frac{1}{Pe_{mz}} = \frac{0.3}{Re Sc} + \frac{0.5}{\left(1 + \frac{3.8}{Re Sc}\right)} \quad [83]$$

$$0.008 < Re < 400, 0.28 < Sc < 2.2$$

A2.7.3 Bischoff & Levenspiel (1962)

$$\frac{1}{Pe_{mz}} = \frac{\varepsilon}{\tau Re Sc} + \frac{0.45}{\left(1 + \frac{7.3}{Re Sc}\right)} \quad [84]$$

A3: Thermal Properties

A3.1 Thermal conductivity

The thermal conductivity of species present in the system has to be evaluated to be used in the modelling of the system. A relatively large part of the reactor consists of open space and thus heat transfer due to forced convection will have a big influence on the effective overall heat transfer of the system. The following temperature dependant equation was used to evaluate the individual thermal conductivity:

$$k_{g,i} = A + B.T + C.T^2 \quad [85]$$

The following table supplies coefficients A, B and C for the various gas species (Yaws, 1999).

Table A-1: Thermal conductivity coefficients

	A	B	C
SO ₃	-0.00354	5.02x10 ⁻⁵	-5.55x10 ⁻⁹
SO ₂	-0.00394	4.48x10 ⁻⁵	2.11x10 ⁻⁹
O ₂	-0.00121	8.62x10 ⁻⁵	-1.33x10 ⁻⁸
H ₂ O	0.00053	4.71x10 ⁻⁵	4.96x10 ⁻⁸
N ₂	0.008	6.00x10 ⁻⁵	-5x10 ⁻⁹

The combined thermal conductivity of the various gases was evaluated by using the following equation:

$$\lambda_{m,f} = \sum \frac{y_i \lambda_i}{\sum y_i A_{ij}} \quad [86]$$

Where:

$$A_{ij} = \frac{1}{4} \left\{ 1 + \sqrt{\frac{\mu_i}{\mu_j} \left(\frac{M_j}{M_i} \right)^{\frac{3}{4}} \left(\frac{T + S_i}{T + S_j} \right)} \right\}^2 \left(\frac{T + S_{ij}}{T + S_i} \right) \quad [87]$$

$$S_i = 1.5 * T_{bi} \quad [88]$$

$$S_{ij} = S_{ji} = C (S_i S_j)^{0.5} \quad [89]$$

A3.2 Dynamic Viscosity

The dynamic viscosity in the packed bed needs to be evaluated in order to account for the resistance caused by friction due to flow. The dynamic viscosity was needed to evaluate the reactor models. The following equation was used to determine the individual dynamic viscosities:

$$\mu_{g,i} = A + B.T + C.T^2 \quad [90]$$

The following table supplies the coefficients for all the species to be used in equation (Yaws, 1999).

Table A-2: Dynamic viscosity coefficients

	A	B	C
SO ₃	-12.039	5.43x10 ⁻¹	-1.60x10 ⁻⁴
SO ₂	-11.103	5.02x10 ⁻¹	-1.08x10 ⁻⁴
O ₂	44.224	5.62x10 ⁻¹	-1.13x10 ⁻⁴
H ₂ O	-36.826	4.29x10 ⁻¹	-1.62x10 ⁻⁴
N ₂	9x10 ⁻⁶	4x10 ⁻⁸	-4x10 ⁻¹²

Appendix A: Transport Properties Correlations

The combined heat dynamic viscosity from all species was calculated by the following:

$$\mu_{m,f} = \frac{\sum y_i \mu_i}{\sum y_i \phi_{ij}} \quad [91]$$

Where:

$$\phi_{ij} = \frac{\left[1 + \left(\mu_i / \mu_j \right)^{0.5} \left(M_j / M_i \right)^{0.25} \right]^2}{\left[8 \left(1 + M_i / M_j \right) \right]^{0.5}} \quad [92]$$

$$\phi_{ji} = \left(\mu_j / \mu_i \right) \left(M_i / M_j \right) \phi_{ij} \quad [93]$$

A3.3 Heat Capacity

The amount of energy required to change the temperature of any substance by a desired amount i.e. heat capacity was evaluated to account for the change in temperature due to heat flux from the wall, as well as dissipation of heat due to reaction. The following equation was used to evaluate the heat capacity:

$$C_p = A + B.T + C.T^2 + D.T^3 + \frac{E}{T^2} \quad [94]$$

The following table supplies coefficients for all gas species to be used in equation 94 above.

Table A-3: Heat capacity coefficients

	A	B	C	D	E
SO ₃	24.025	119.461	-94.387	26.962	-0.116
SO ₂	21.430	74.351	-57.752	16.355	0.087
O ₂	29.659	6.137	-1.187	0.096	-0.220
H ₂ O	30.092	6.833	6.793	-2.534	0.082

Appendix A: Transport Properties Correlations

N ₂	19.5	19.88	-8.598	1.369	0.5276
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The combined heat capacity was the sum of the each species multiplied by the molar fraction:

$$c_{p,m} = \sum y_i c_{p,i} \quad [95]$$

A3.4 Density

The density of the various species was calculated using the ideal gas law. The following equation was used to account for each of the individual gas species:

$$\rho_i = \frac{P.M_{w,i}}{R.T} \quad [96]$$

A3.5 Titanium Dioxide

The TiO₂ used in this study contains 75% anatase and 25% rutile phase as already mentioned. The solid density was taken as the combined fraction of each phase multiplied by that specific density. A density of 2 406 kg/m³ was obtained for a void fraction of 0.39 evaluated from BET analysis. Incropera & De Witt (2002) supplies thermal conductivity and heat capacity values at different temperatures. These values were used by fitting a second order polynomial through the data. The following two equations were used to represent the heat capacity and thermal conductivity of TiO₂:

$$k_s = 8e^{-6}T^2 - 0.0166T + 12.37 \quad [97]$$

$$c_{p,s} = 4e^{-7}T^3 - 0.0012T^2 + 1.2798T + 464 \quad [98]$$

A3.6 Heat of Reaction

The heat of reaction is the energy required to thermodynamically split a molecule of SO₃ into SO₂ and 0.5 O₂. The heat of reaction given at reference temperature is 98.92 kJ/mol ($T_R = 298$ K). To account for the operating temperature the change in heat capacity will account for the change in heat absorbed to

Appendix A: Transport Properties Correlations

decompose SO_3 . The following equation can be utilized to describe the heat of reaction at changing operating temperature conditions (Smith, 2001):

$$\Delta H_{\text{Rx}}(T) = \Delta H_{\text{Rx}}^0(T_R) + \int_{T_R}^T \Delta c_p dT \quad [99]$$

A4: GC calibration Standard Gases

The standard GC calibration gases were obtained from AFROX and Table A-4 includes volume/molar percentage of the gas sample content.

Table A-4: GC calibration standard gases

Gas	SO ₂	O ₂	N ₂
1	1	0.5	98.5
2	10	5	85
3	50	25	25

B. Appendix B: Micro Pellet Reactor Model

B1: Physical Properties

The physical values for all parameters used in the CFD model can be found in Table B-1:

Table B-1: Catalyst pellet CFD model parameter values

	Fluid					Solid			
Parameter	923	973	1023	1 073	Parameter	923	973	1 023	1 073
Concentration									
ρ_b	100	100	100	100	ε_p	0.16	0.16	0.16	0.16
D_{eff}	4.65e-5	5.19e-5	5.6e-5	6.1e-5	ρ_b	2520	2520	2520	2520
C_{a0}	0.98	0.93	0.89	0.85	D_{efs}	4.72e-5	5.19e-5	5.2e-5	4.85e-5
C_{b0}	0	0	0	0	C_{as0}	0	0	0	0
C_{c0}	0	0	0	0	C_{bs0}	0	0	0	0
C_{i0}	0.74	0.72	0.69	0.65	C_{cs0}	0	0	0	0
C_{n0}	10.06	9.5	9.04	8.62	C_{is0}	0	0	0	0
					C_{ns0}	0	0	0	0
					D_k	4.95e-6	5.07e-6	5.2e-6	5.32e-6
					$D_{eff,m}$	4.3e-7	4.5e-7	4.64e-7	4.7e-7
					τ	1.43	1.43	1.43	1.43
Thermal									

Appendix B: Micro pellet Reactor Model

λ_f	0.06	0.062	0.065	0.069	λ_s	3.5	3.5	3.5	3.5
λ_{gw}	0.1	0.1	0.1	0.1	$c_{p,s}$	900	905	910	915
$\bar{M}_w$	0.019	0.019	0.019	0.019	$T_{s,0}$	923	973	1023	1073
$c_{p,f}$	34.59	34.12	34.48	35.77	ρ_s	2520	2520	2520	2520
T_0	923	973	1023	1073					
P_0	87.3	87.3	87.3	87.3					
ρ_f	0.34	0.316	0.30	0.293					
μ_f	4e-5	4.2e-5	4.38e-5	4.53e-5					

B2: Particle Sizes

Table represents the physical sizes of the particles used in the experiments and model together with some experimental values.

Table B-2: Catalyst pellet sizes used in experiments and model

	1	2	3	4	5	T (°C)	U (m/s)	Ra (mol/m ³ .s)	WHSV (h ⁻¹)
hp	4.7	5.1	4.48	4.12	4.1	750	0.95	144.85	60
dp	1.6	1.68	1.56	1.6	1.82				
2									
hp	4.12	4.1	4.56	5.02	3.9	750	0.95	299.7	178

Appendix B: Micro pellet Reactor Model

dp	1.68	1.66	1.6	1.6	1.52				
3									
hp	3.94	4.14	3.94	3.96	5.17	750	0.95	336	320
dp	1.6	1.68	1.68	1.64	1.56				
4									
hp	4.28	4.74	4.86	4.96	4.78	750	0.95	322	343
dp	1.64	1.62	1.56	1.66	1.6				
5									
hp	4.14	4.74	4.96	5.16	4.36	800	1	159	56
dp	1.52	1.63	1.64	1.6	1.6				
6									
hp	4.2	5.22	5.12	4.96	5.1	800	1	468	268
dp	1.61	1.64	1.62	1.55	1.54				
7									
hp	4	4.52	3.88	5	4.5		1	560	391
dp	1.52	1.56	1.6	1.6	1.72	800			
8									
hp	5.1	3.8	4.21	4.96	3.34	800	1	336	182
dp	1.64	1.66	1.64	1.54	1.66				
9									
hp	3.6	4.7	4.12	5.6	3.98	700	0.91	111	66

Appendix B: Micro pellet Reactor Model

dp	1.58	1.58	1.42	1.58	1.6				
10									
hp	5.3	4.56	5	5.02	3.9	700	0.91	163	171
dp	1.6	1.58	1.64	1.58	1.68				
11									
hp	4.33	5.42	5.2	4.1	5.1	700	0.91	176	272
dp	1.66	1.64	1.66	1.66	1.7				
12									
hp	4.54	5	5.6	5.08	4.59	700	0.91	171	326
dp	1.4	1.88	1.66	1.64	1.58				
13									
hp	4.66	4.54	4.38	4.68	5.2	650	0.86	50	57
dp	1.64	1.72	1.58	1.56	1.62				
14									
hp	5.14	5.1	4.48	4.35	4.54	650	0.86	94	170
dp	1.6	1.62	1.66	1.63	1.65				
15									
hp	4.22	4.42	5	4.74	4.98	650	0.86	91	294
dp	1.6	1.58	1.68	1.58	1.6				
16									
hp	4.84	4.14	5.34	5.6	4.12	650	0.86	67	327

Appendix B: Micro pellet Reactor Model

dp	1.6	1.58	1.68	1.72	1.58				
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B3: Supplementary CFD Results

Additional results generated in the catalyst pellet model using COMSOL Multi-Physics® 4.3b include velocity distribution and concentration distribution. Velocity distribution can be seen in Figure B-1.

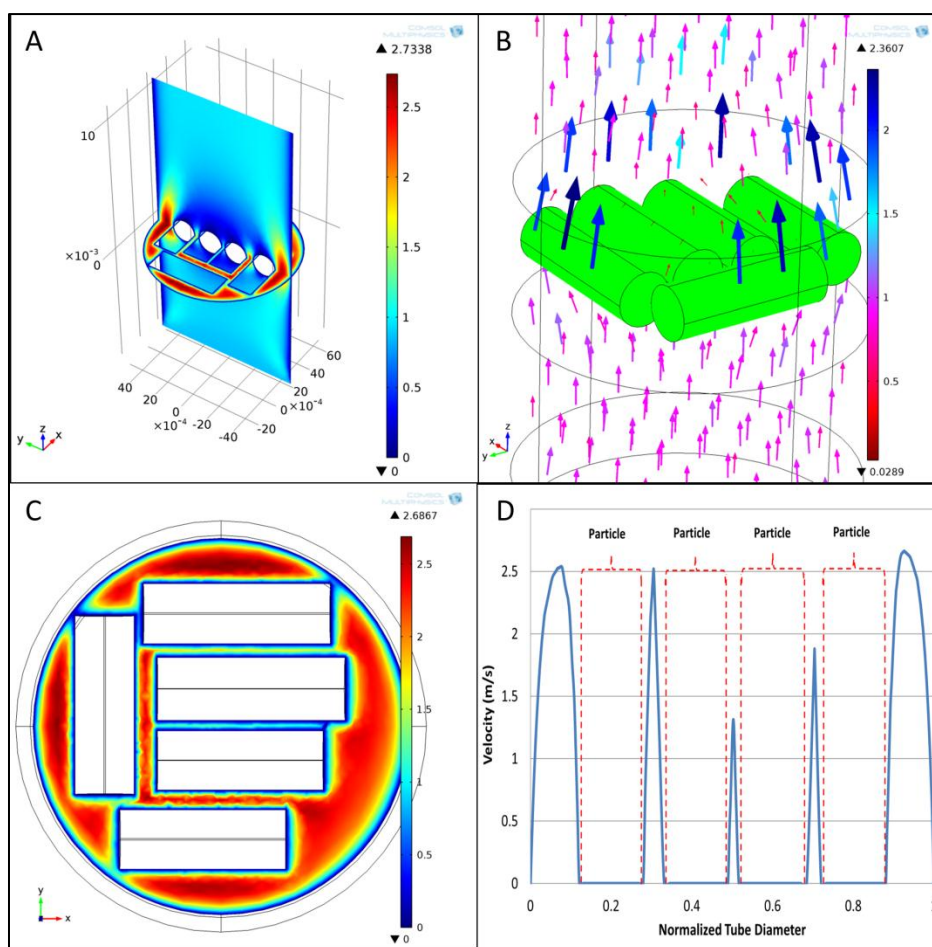


Figure B-1: Model Results; A: Cross sectional (axial & radial) velocity distribution (m/s); B: Streamline velocity distribution through the porous media (m/s); C: Cross sectional (radial) velocity distribution (m/s); D: Centreline velocity profile (m/s)

Appendix B: Micro pellet Reactor Model

Concentration distribution of sulphur trioxide (A), sulphur dioxide (B) and oxygen (C) can be seen in Figure B-2.

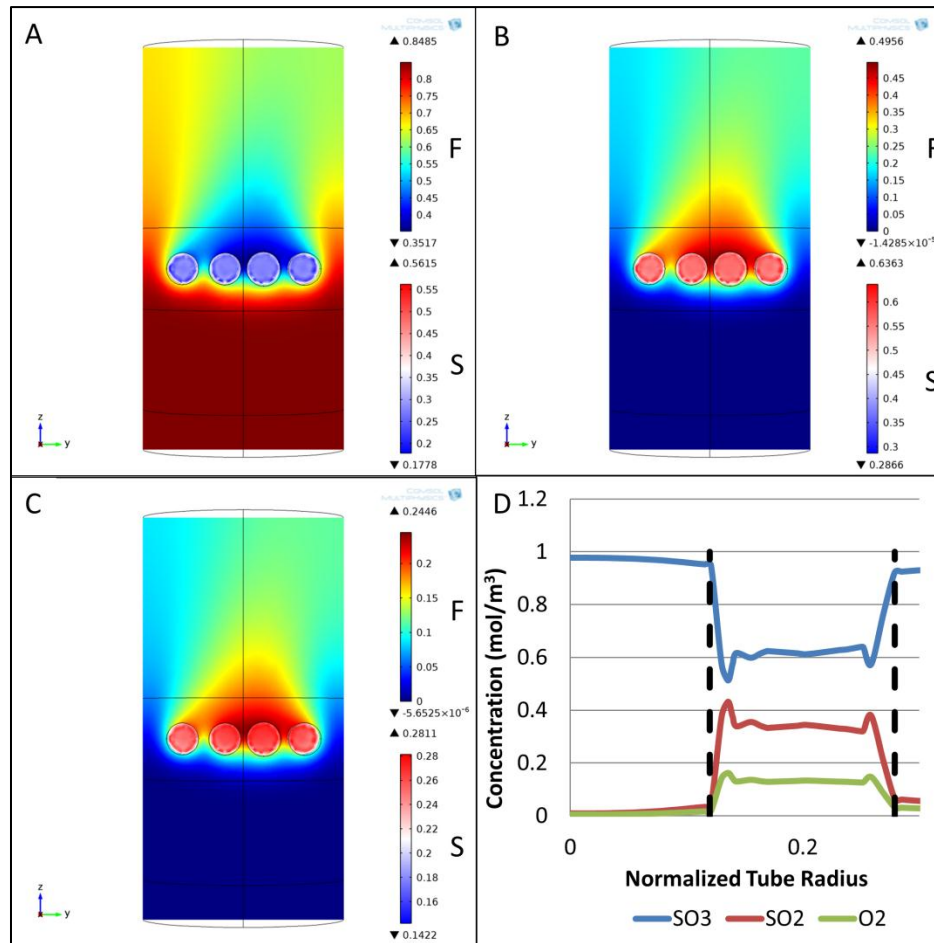


Figure B-2: 2D Cross sectional results for concentration 1 at temperature 1 073 K inlet; A: Concentration distribution of SO_3 (mol/m^3); B: Concentration distribution of SO_2 (mol/m^3); C: Concentration distribution of O_2 (mol/m^3); D: Centreline concentration profile through fluid and one particle (F indicates fluid phase and S solid phase)

Appendix B: Micro pellet Reactor Model

Concentration distribution on the surface of the catalyst particles for sulphur trioxide (A), sulphur dioxide (B) and oxygen (C) can be seen in Figure B-3.

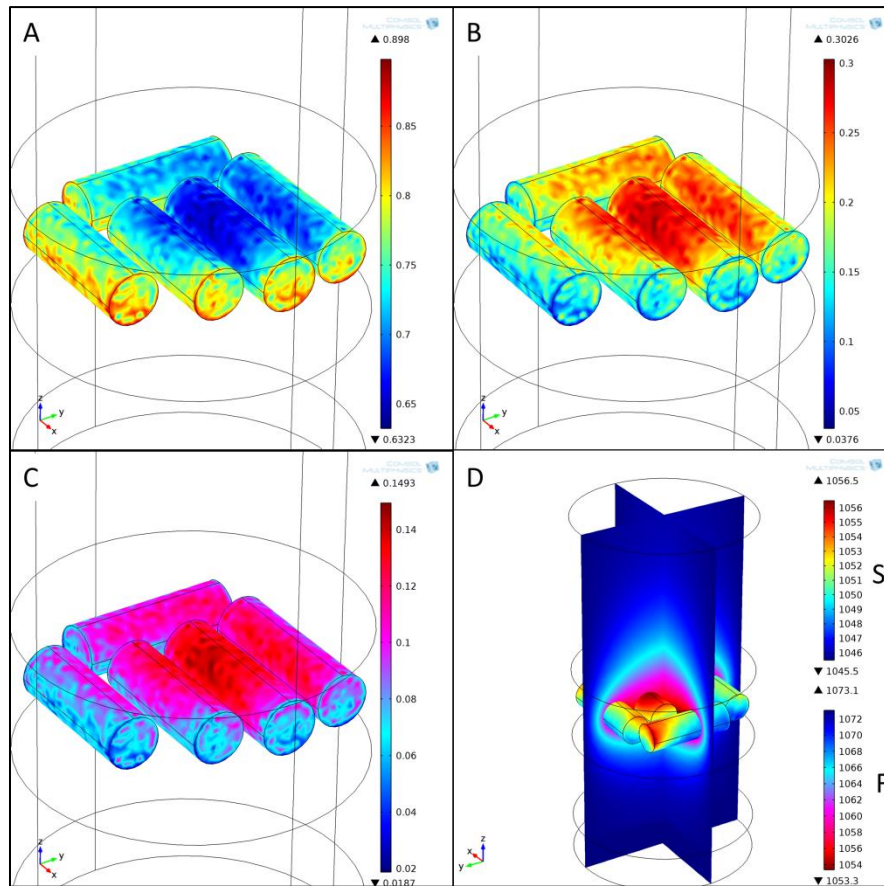


Figure B-3: Distribution on surface of particles; A: Concentration of SO_3 (mol/m^3); B: Concentration of SO_2 (mol/m^3); C: Concentration of O_2 (mol/m^3); D: Temperature distribution on surface of particles as well as fluid (K) (F indicates fluid phase and S solid phase)

C. Appendix C: Porosity and Void Fraction Calculations

The definition of porosity is said to be the volume of open pores per total volume of solid (Gregg, 1982). The porosity of a porous catalyst particle can be evaluated by N₂ or CO₂ physi-sorption by BET analysis. In order to determine this porosity the incremental volume change absorbed per pore width range has to be integrated over the entire pore range. This can be accomplished by using the following equation:

$$\varepsilon_0 = \rho_b \int \left(\frac{dV}{dD_{pore}} \right) dD_{pore} \quad [100]$$

The BET analysis was completed by UCT. The bulk density was evaluated by inserting an amount of catalyst in a 50 mL measuring flask with the same inner diameter as the reactor. The flask was filled with catalyst up to the 50 mL mark. The amount of catalyst was weighed without moving the flask as to ensure the same random packing. This was done for six times to get an average weight per volume flask. This resulted in a bulk density of 995 kg/m³ and a particle density (Taking TiO₂ density of 4000 kg/m³) of 2 443 kg/m³. Dividing the bulk density by the particle density, the void fraction for the reactor was found to be 0.4074. This value was compared to a theoretical equation used to evaluate the void fraction for cylindrical particles. The following equation was used (Adams, 2009):

$$\varepsilon_b = 0.38 + 0.073 \left[1 - \frac{(d_t/d_p - 2)^2}{(d_t/d_p)^2} \right] \quad [101]$$

The equation gave a void fraction of 0.4012. This equation gives an accurate representation of the void fraction in the bed with an error of 1.67% for the values of the fresh catalyst. The results obtained for void fractions of particle and bed can be seen in Table C-1.

Table C-1: Void fraction and particle density

	Fresh	Spent
ρ_B (kg/m ³)	995	1177
ρ_p (kg/m ³)	2443	3325

Appendix C: Porosity and Void Fraction

ε_b	0.4074	0.35
ε_0	0.3892	0.2012

D. Appendix D: Heat and Mass Transfer Criteria

The fluid flow around the particle with the interaction of heat and mass between the fluid phase and the solid phase can simplify or complicate reactor modelling and kinetic evaluation of a catalyst. As mentioned in Chapter 2 certain criteria can be used to eliminate certain effects on the catalyst and in turn simplify the numerical mathematical model to be solved. During this study different forms of the catalyst were utilized, including:

- Single solid catalyst particles
- A packed bed of particles

The criteria of Mears as mentioned in Chapter 2 will be discussed with relation to the experimental conditions for the three different scenarios mentioned above.

D1: Overall Particle Model

The 5 catalyst pellets were used to evaluate the kinetics for the reaction and the influence of heat and mass transfer were evaluated. The conditions and values for concentration 1 are given in the following tables. Due to the amount of data and similarities other experimental runs criteria will not be given.

Table: D-1: Interfacial gradients for particles (Concentration 1)

	Temperatures				Unit
	923	973	1023	1073	K
r_{eff}	91	176	336	468	mol/m ³ .s
C_{A0}	0.99	0.94	0.89	0.85	mol/m ³
k_s	0.95	0.96	0.94	0.96	m/s
n	1	1	1	1	-
h_s	75	64	67	65	W/m ² .s
Ar	25.54	24.23	23.04	21.97	

Appendix D: Heat and Mass Transfer Criteria

Heat Criteria	2.6	5.2	9.2	11.6	
Mass Criteria	0.08	0.15	0.28	0.45	

The criteria for concentration and heat gradients between the fluid and solid are given as:

$$\left| \frac{r_{eff} d_p}{2C_{A0} k_s} \right| < \frac{0.15}{n} \quad [102]$$

$$\left| \frac{-\Delta H_{Rx} r_{eff} d_p}{2T_0 h_s} \right| Ar < 0.15 \quad [103]$$

Intra-particle gradients

Table D-2: Intra-particle gradients for particles (Concentration 1)

	Temperatures				Unit
	923	973	1023	1073	K
D_{eff}	6.5x10-7	1.66x10-6	4.5x10-7	1.49x10-7	m ² /s
C_s	0.99	0.94	0.89	0.85	mol/m ³
λ_c	3.5	3.5	3.5	3.5	W/m.K
T_s	923	973	1023	1073	K
T_c	922.98	972.9	1022.9	1073	K
Criteria	91	67	571	2374	

The intra-particle mass and heat transfer gradients can be neglected if the following is true:

$$Da_{II} |n - Ar.P_t| < 1 \quad [104]$$

Where the Damkohler group 2 which gives the ratio between chemical rate and molecular diffusion and Prater number (maximum intra-particle temperature rise):

$$Da_{II} = \frac{r_{eff} d_p^2}{4D_{eff} C_s} \quad [105]$$

$$P_t = \frac{-\Delta H_{Rx} D_{eff} C_s}{\lambda_e T_s} \quad [106]$$

From the criteria used to describe concentration 1 (Chapter 4) it can be seen (Table: D-1 & Table D-2) that the criteria are satisfied for an inlet temperature 923K. All the other criteria are not satisfied which means inter and intra-particle heat and mass transfer effects are prominent.

D1.2 Effect of Pore Diffusion

To determine if the diffusion inside of the catalyst particles are limiting the Wagner-Weisz-Wheeler modulus can be used with measured quantities to indicate whether this effect is severe (Levenspiel, 1999):

$$M_w = L^2 \frac{(-r_A''' / C_A)_{obs}}{D_e} \quad [107]$$

When $M_w < 0.15$ the particles are in diffusion-free regime while if $M_w > 4$ the particles are in a strong pore diffusion regime.

Table D-3: W-W-W criteria for pore diffusion

	Temperature		Units
	923	1073	K
Criteria	22.9	593	

The WWW modulus was evaluated for the highest and lowest temperature of concentration 1 and it was found that there were strong resistance to pore diffusion. The results for concentration 2 are not shown since similar results were obtained.

D2: Packed Bed Model

The packed bed consisted of a bed of particles where the aspect ratio was approximately 13. The criteria for interfacial gradients, as well as intra-particle gradients were evaluated in the same manner as for the particle model described above. Two additional gradient evaluations have to be conducted for the large fixed bed which includes axial and radial dispersion of heat and mass. Axial dispersion in a packing may be as a result of the packing structure that the mixing of the fluid becomes severe. To evaluate this effect the Mears criterion was used to evaluate whether axial dispersion should be accounted for. The following criteria can be used to determine if this effect is negligible:

$$\left| \frac{n.Da_I}{Pe_{a,m}} - \frac{Ar.Da_{III}}{Pe_{a,h}} \right| < 0.05 \quad [108]$$

Where:

- $Da_I = \frac{r_{eff} d_p}{u_s C_{a0}}$; Damkohler group 1
- $Da_{III} = \frac{-\Delta H_{Rx} r_{eff} d_p}{\rho_f u_s T_w c_p}$; Damkohler group 3
- $Pe_{a,m} = \frac{u_s d_p}{D_a}$; Peclet number for mass
- $Pe_{a,h} = \frac{\rho_f u_s d_p c_p}{\lambda_a}$; Peclet number for heat

If the condition is satisfied axial dispersion may be neglected from the model. The next criterion are that for radial dispersion of heat and mass. The effects of radial dispersion are quite an important one as it has the possibility to reduce a model with a dimension; from 2D to 1D. The criterion are as follows:

$$\left| \frac{-\Delta H_{Rx} r_{eff}^* d_t^2}{\lambda_r T_w} \right| . Ar < \frac{1.6}{1 + \frac{8}{Bi_w}} \quad [109]$$

Where:

- $Bi_w = \frac{\alpha_w d_t}{\lambda_{eff,r}}$

Appendix D: Heat and Mass Transfer Criteria

The mass and heat dispersion coefficients in the axial direction were calculated by the correlations provided by Wen & Fan (1975) and Dixon and Cresswell (1979) respectively. Effective radial thermal conductivity was equated by Bauer and Schlünder (1978) and radial diffusivity was also equated by Bauer and Schlünder (1978).

Interfacial gradients:

Table D-4: Interfacial gradients for packed bed

	Temperatures		Unit
	903	1053	K
r_{eff}	4.83	8.05	mol/m ³ .s
C_{A0}	3.19	1.81	mol/m ³
k_s	0.205	0.237	m/s
n	1	1	-
h_s	280	287	W/m ² .s
Ar	26.11	22.39	
Heat Criteria	0.03	0.07	
Mass Criteria	0.0093	0.0237	

Intra-particle gradients:

Table D-5: Intra-particle gradients for packed bed

	Temperatures		Unit
	903	1053	K

Appendix D: Heat and Mass Transfer Criteria

D_{eff}	1.43×10^{-7}	1.6×10^{-7}	m^2/s
C_s	3.19	1.81	mol/m^3
λ_c	3.5	3.5	$W/m.K$
T_s	903	1053	K
T_c	902.9	1052.9	K
Criteria	16.74	43.85	

Axial Dispersion:

Table D-6: Axial dispersion criteria for packed bed

	Temperatures		Units
Parameter	903	1053	K
Da_I	1.71×10^{-3}	2.26×10^{-3}	-
Da_{III}	0.0017	0.0022	-
Pe_{am}	0.18	0.18	-
Pe_{ah}	1.75	1.72	-
u_s	1	1.32	m/s
ρ_g	0.58	0.50	kg/m^3
C_p	1843	1905	$J/kg.K$
T_w	903	1053	K

Appendix D: Heat and Mass Transfer Criteria

D_a	0.0149	0.0188	m ² /s
λ_a	1.12	1.23	W/m.K
Criteria	0.004	0.005	

Radial Dispersion:

Table D-7: Radial dispersion criteria for packed bed

	Temperatures		K
	903	1053	Units
r_{eff}^*	5.8	9.6	mol/m ³ .s
λ_r	59.1	65.9	W/m.K
Bi_w	0.27	0.27	-
α_w	766	854	W/m ² .K
$\lambda_{eff,r}$	60.19	66.9	W/m.K
Pe_r	11.39	11.39	-
d_t	0.0209	0.0209	m
N	8.31	8.31	-
Criteria	0.12	0.14	

E. Appendix E: Thermodynamic Equilibrium Conversion

E1: Kinetic Setup Equilibrium Conversion

The sulphur trioxide decomposition reaction is a reversible reaction and thus at specific reaction conditions the forward and backward rate of the reaction will be the same. The sulphur trioxide equilibrium conversion without any inert species and with nitrogen as inert carrier was calculated thermodynamically to evaluate whether the system is close to equilibrium conditions.

Pure SO₃ equilibrium conversion:

The method in Smith and Van Ness (Smith, 2001) was used to do evaluate the equilibrium conversion curves at different pressure as a function of temperature. The equation given for equilibrium constant includes Gibbs energy, Heat of reaction and Heat capacity as follows:

$$\ln K = -\frac{\Delta G^o}{RT} \quad [110]$$

Where:

$$\frac{\Delta G^o}{RT} = \frac{\Delta G_0^o - \Delta H_0^o}{RT_0} + \frac{\Delta H_0^o}{RT} + \frac{1}{T} \int_{T_0}^T \frac{\Delta C_p^0}{R} dT - \int_{T_0}^T \frac{\Delta C_p^0}{R} \frac{dT}{T} \quad [111]$$

The equilibrium expression displaying the pressure and composition is given as:

$$\prod (y_i \hat{\phi}_i)^{v_i} = \left(\frac{P}{P_0} \right)^{-v} K \quad [112]$$

In Equation 112 above the pressure divided by the standard pressure of 1 bar to the power of the total molar fraction of system. This is equal to the sum of the molar fraction of species multiplied by the fugacity for that specie. The fugacity of species was calculated by the following equation:

$$\phi = \exp \left(\frac{P_r}{T_r} (B^0 + \omega B^1) \right) \quad [113]$$

With:

$$B^0 = 0.083 - \frac{0.422}{T_r^{1.6}} \quad [114]$$

$$B^1 = 0.139 - \frac{0.172}{T_r^{4.2}} \quad [115]$$

All the values needed for pure species is obtained in tables from Smith and Van Ness. The following figure was generated using the equations given above to determine the equilibrium conversion as a function of temperature at different pressures:

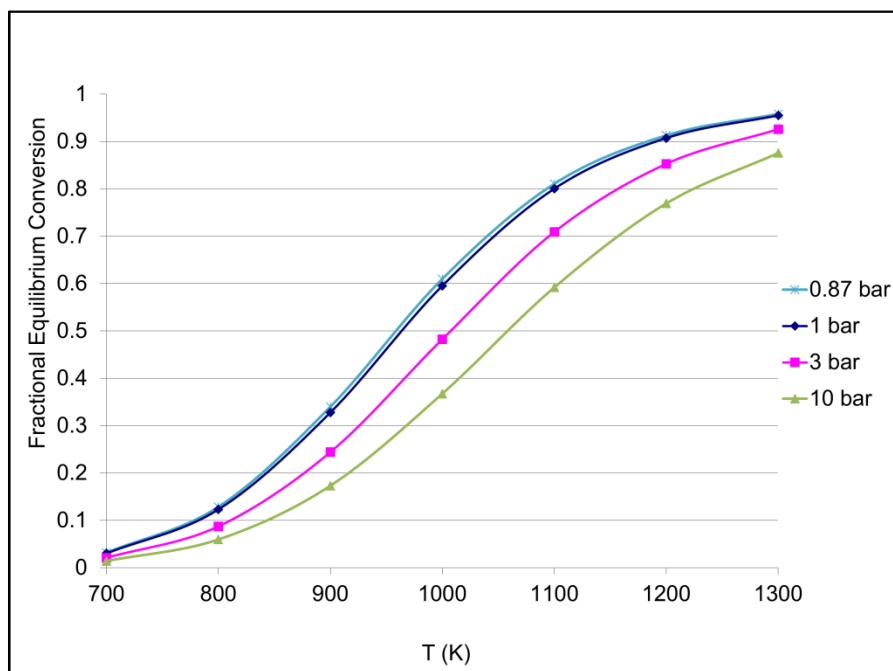


Figure E-1: Equilibrium conversion for pure SO_3 at different pressure as a function of temperature

H_2SO_4 equilibrium conversion with inert Nitrogen:

The total decomposition of H_2SO_4 is a very difficult objective to quantify experimentally as the acid in decomposed form, SO_3 and H_2O , has the tendency in the absence of heat to combine and form acid again. In the work of Kondamudi & Upadhyayula (2010) they did some simulations on Aspen HYSYS V7.1 using a Gibbs type reactor with the Peng-Robinson-Stryjek-Vera and modified Peng-Robinson equation of state so that ideal gas approximation need not be used. The same approach was followed during this study to determine the equilibrium conversion and the shift in equilibrium conversion due to the

Appendix E: Thermodynamic Equilibrium Conversion

presence of inert nitrogen in the feed stream. The SRK equation of state and NRTL was used to evaluate the equilibrium conversion. The first simulation entailed the equilibrium conversion of pure sulphuric acid at different temperatures. The following figure depicts conversion of pure sulphuric acid as a function of temperature at different pressures.

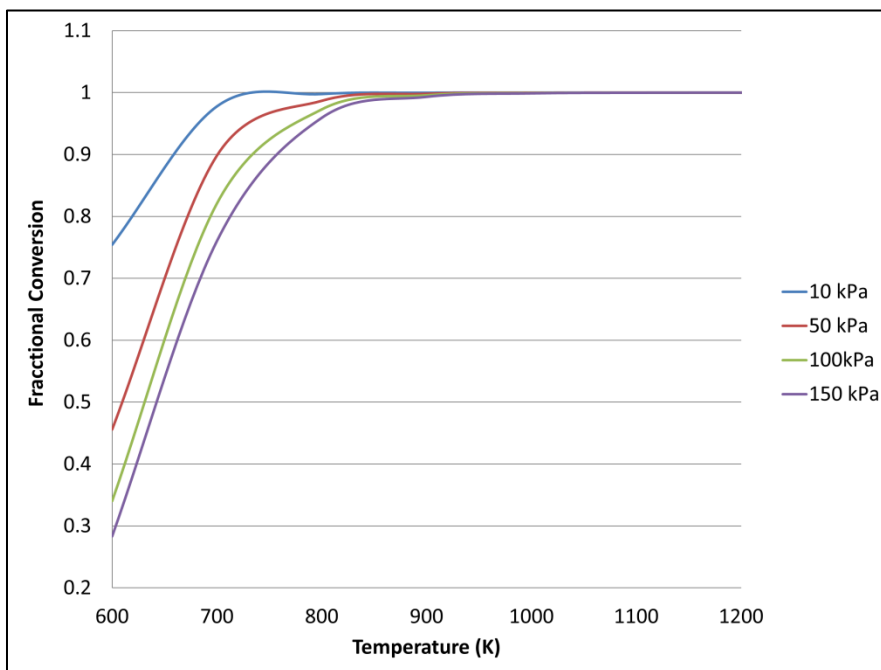


Figure E-2: Equilibrium conversion for pure H_2SO_4 at different pressure as a function of temperature

The experimental setup, however, does not only contain pure H_2SO_4 but also inert nitrogen to increase flow rate to ensure enough flow goes through to the gas analyser, to dilute the gas stream due to the limitations of percentage gas analysed in the gas analyser and to ensure WHSV can be increased without increasing acid flow and possibly cause overflow in traps. The same approach was followed and the following graph represents the decomposition of H_2SO_4 and nitrogen in the molar ratio as in the catalyst experiments.

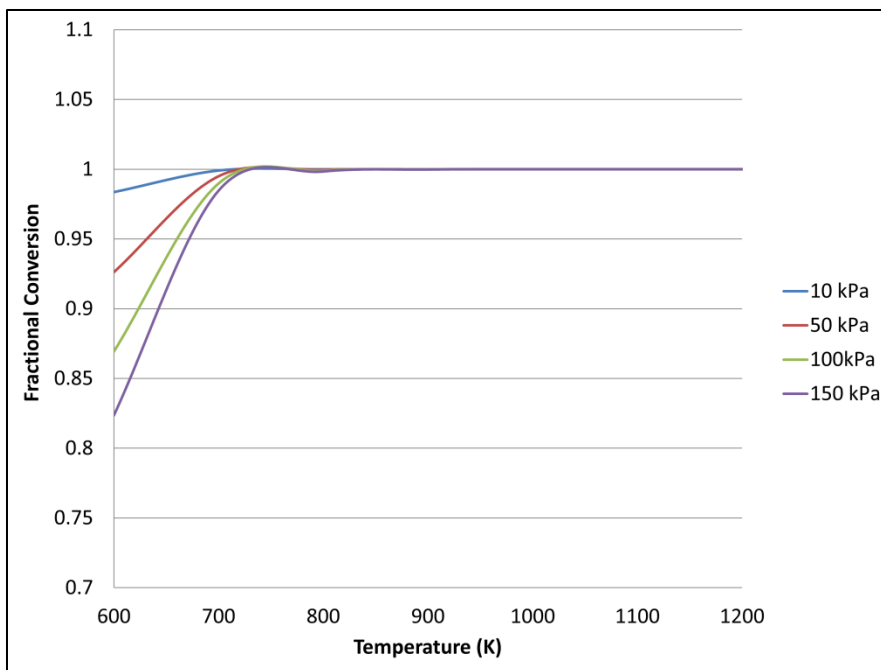


Figure E-3: Equilibrium conversion of H_2SO_4 with inert nitrogen

For the sulphuric acid decomposition reaction the NRTL equation of state was used. From Figure E-3 and Figure E-2 it can be seen that the inert nitrogen shifts the equilibrium conversion and enhances the decomposition reaction due to the principle of Le Chatelier. Thus with the flow conditions of the kinetic setup the assumption can be valid that all sulphuric acid is decomposed at start of catalyst bed and only SO_3 and H_2O present.

SO_3 with inert nitrogen for powder kinetics:

The influence of nitrogen on the equilibrium conversion was calculated thermodynamically. Various equations of state were used in simulations but did not differ to a great extent. For the specific molar feed ratio of SO_3 , H_2O and N_2 the equilibrium conversion for different pressures as a function of temperature can be seen in Figure E-4.

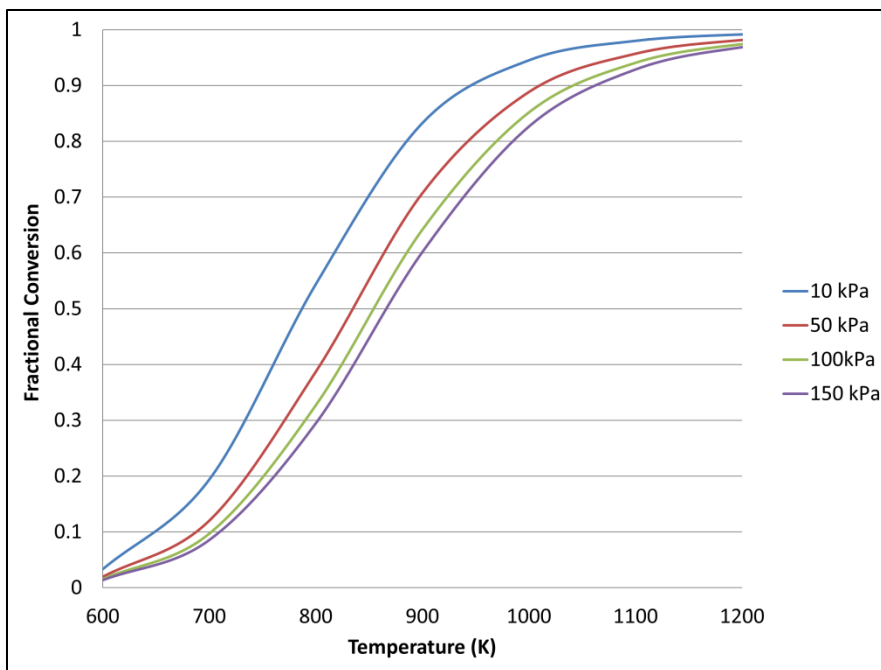


Figure E-4: Equilibrium conversion of feed composition to differential bed at different pressure as a function of temperature

The reason for only evaluating equilibrium conversion at low pressure is that for the kinetic setup the process conditions were chosen to be atmospheric and the setup used could not work under pressure due to the quartz couplings not being able to withstand high pressure. From Figure E-3 and Figure E-4 it can be seen that inert nitrogen increases the equilibrium conversion by a significant margin. The results obtained from Aspen HYSYS simulations compared very well with the work from *Kondamudi & Upadhyayula (2010)*.

SO₃ with inert nitrogen for particle kinetics:

The equilibrium conversion was equated as described above for the particle kinetics process conditions. The variable was the inlet concentration and the temperature. Thus the pressure was taken to be constant as 83.7 kPa throughout. The results obtained can be seen in Figure E-5 for the equilibrium conversion as a function of temperature for the 4 different inlet conditions.

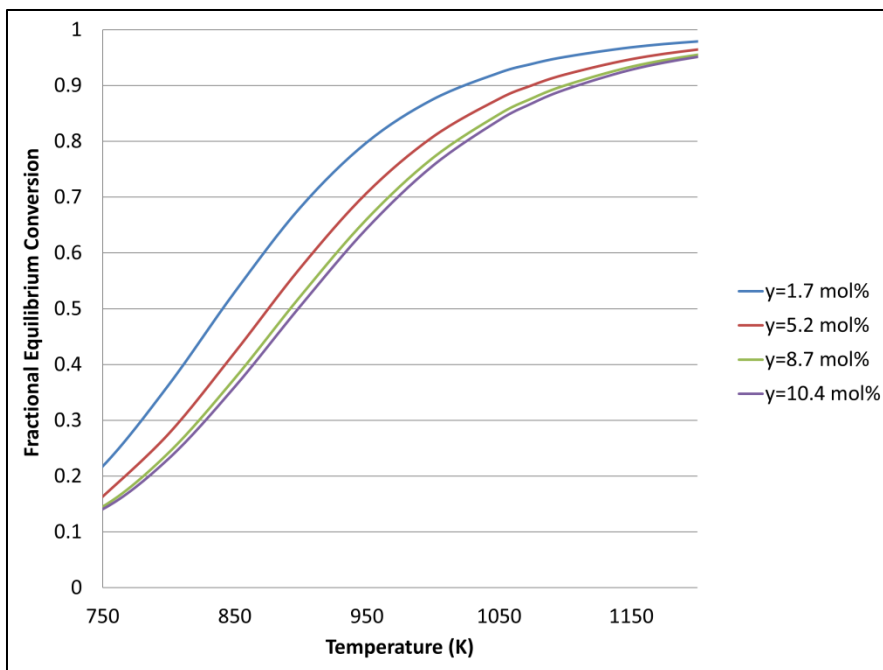


Figure E-5: Equilibrium conversion of particle kinetics for different inlet concentrations as a function of temperature and constant inlet pressure

E2: Packed Bed Setup Equilibrium Conversion

Variable WHSV:

The equilibrium conversion was equated in the same manner as described in Section E.1 above in an Aspen Model. In this section some equilibrium graphs were generated for the variation in WHSV, specifically the 3 and 4 ml/min acid flow rates. These graphs can be seen in Figure E-6 and Figure E-7 where the equilibrium conversion is given as a function of temperature for different operating pressure. Since the process conditions of the fixed bed system varied much and specifically the amount of pre-conversion achieved, as well as the operating temperature, the equilibrium conversion was equated for all individual experimental results. All the data will not be given here but the specific values are given in the applicable graphs in Chapter 6.

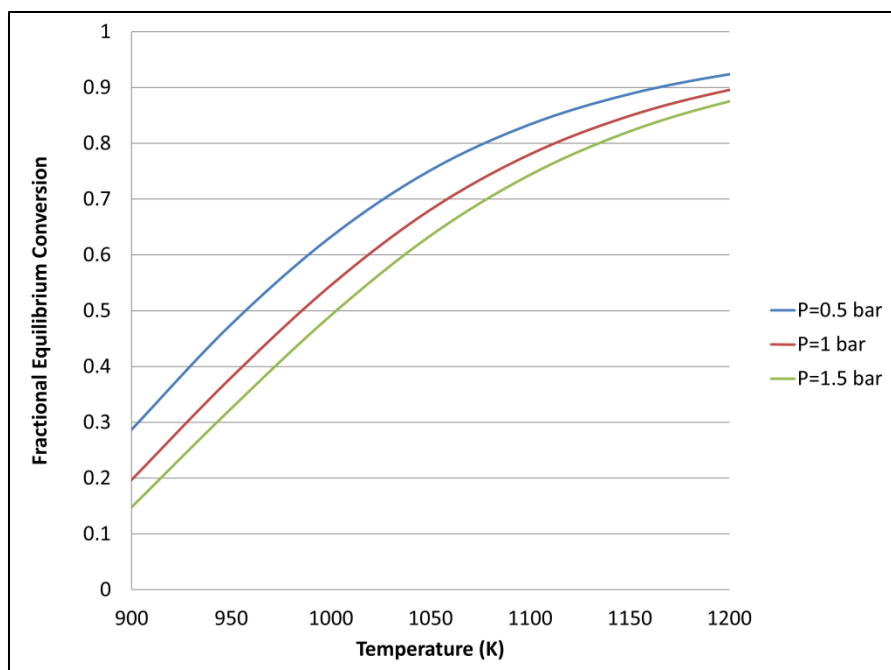


Figure E-6: Equilibrium conversion for variable WHSV process conditions as a function of pressure (Acid=3 ml/min)

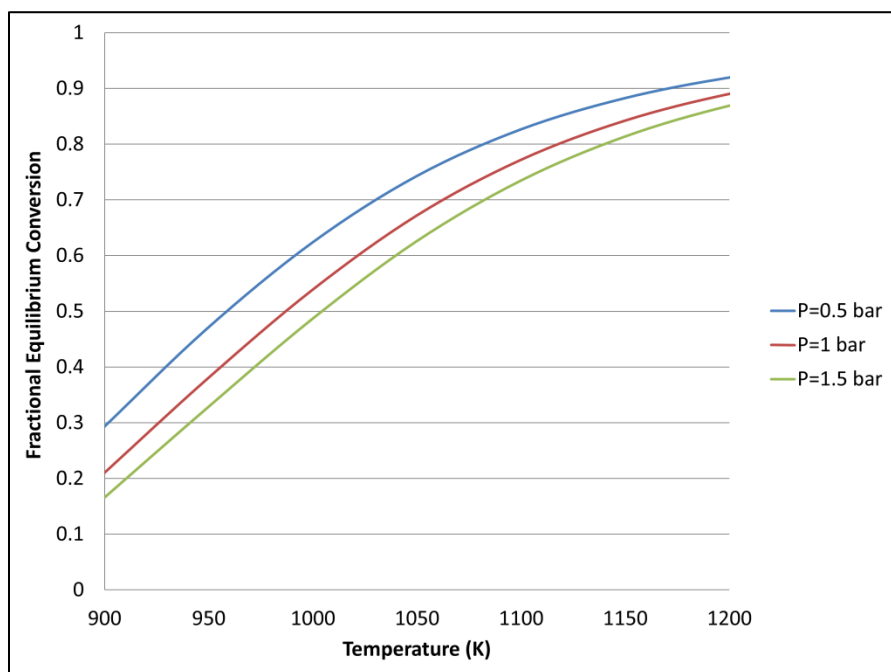


Figure E-7: Equilibrium conversion for variable WHSV process conditions as a function of pressure (Acid=4 ml/min)

F. Appendix F: Reactor Equations

The equations used in the CFD models for the systems are given below in cylindrical coordinates, represented by the Nabla operator in the Chapters.

F1: 3D Particle Model

Solid Phase:

$$D_{efm,r} \left(\frac{\partial^2 C_{s,r}}{\partial r^2} + \frac{1}{r} \frac{\partial C_{s,r}}{\partial r} \right) + D_{efm,\phi} \frac{1}{r^2} \frac{\partial^2 C_{s,\phi}}{\partial \phi^2} + D_{efm,z} \frac{\partial^2 C_{s,z}}{\partial z^2} = r_A$$

$$\lambda_{s,r} \left(\frac{\partial^2 T_{s,r}}{\partial r^2} + \frac{1}{r} \frac{\partial T_{s,r}}{\partial r} \right) + \lambda_{s,\phi} \frac{1}{r^2} \frac{\partial^2 T_{s,\phi}}{\partial \phi^2} + \lambda_{s,z} \frac{\partial^2 T_{s,z}}{\partial z^2} = r_A \cdot \Delta H_{Rx}$$

Fluid Phase:

$$\left[u_r \frac{\partial C_{A,r}}{\partial r} + u_\phi \frac{1}{r} \frac{\partial C_{A,\phi}}{\partial \phi} + u_z \frac{\partial C_{A,z}}{\partial z} \right] = k_m (C_A - C_s)$$

$$\left[u_r \rho c_p \frac{\partial T_{f,r}}{\partial r} + u_\phi \rho c_p \frac{1}{r} \frac{\partial T_{f,\phi}}{\partial \phi} + u_z \rho c_p \frac{\partial T_{f,z}}{\partial z} \right] = h_{fs} (T_w - T_s)$$

Boundary Conditions:

Inside Particle interface

$$\left[D_{efm,r} \frac{\partial C_{s,r}}{\partial r} + D_{efm,\phi} \frac{1}{r} \frac{\partial C_{s,\phi}}{\partial \phi} + D_{efm,z} \frac{\partial C_{s,z}}{\partial z} \right] = k_m (C_A - C_s)$$

$$\left[\lambda_{s,r} \frac{\partial T_{f,r}}{\partial r} + \lambda_{s,\phi} \frac{1}{r} \frac{\partial T_{f,\phi}}{\partial \phi} + \lambda_{s,z} \frac{\partial T_{f,z}}{\partial z} \right] = h_{fs} (T_w - T_s)$$

Wall Temperature Flux

$$\left[\lambda_{f,r} \frac{\partial T_{f,r}}{\partial r} + \lambda_{f,\phi} \frac{1}{r} \frac{\partial T_{f,\phi}}{\partial \phi} + \lambda_{f,z} \frac{\partial T_{f,z}}{\partial z} \right] = h_w (T_f - T_w)$$

Appendix F: Reactor Equations

No flux at tube wall

$$\left[\frac{\partial C_{A,r}}{\partial r} + \frac{1}{r} \frac{\partial C_{A,\phi}}{\partial \phi} + \frac{\partial C_{A,z}}{\partial z} \right] = 0$$

Navier Stokes Porous media:

$$r: \frac{\rho}{\varepsilon_p} \left(\frac{u_r}{\varepsilon_p} \frac{\partial u_r}{\partial r} + \frac{u_\phi}{\varepsilon_p r} \frac{\partial u_r}{\partial \phi} + \frac{u_z}{\varepsilon_p} \frac{\partial u_r}{\partial z} - \frac{u_\phi^2}{r} \right) = -\frac{\partial p}{\partial r} + \frac{\mu}{\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_r}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_r}{\partial \phi^2} + \frac{\partial^2 u_r}{\partial z^2} - \frac{u_r}{r^2} - \frac{2}{r^2} \frac{\partial u_\phi}{\partial \phi} \right] + \frac{2\mu}{3\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_r}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_r}{\partial \phi^2} + \frac{\partial^2 u_r}{\partial z^2} - \frac{u_r}{r^2} - \frac{2}{r^2} \frac{\partial u_\phi}{\partial \phi} \right] - \frac{\mu}{K_{br}} u_r$$

$$\phi: \frac{\rho}{\varepsilon_p} \left(\frac{u_r}{\varepsilon_p} \frac{\partial u_\phi}{\partial r} + \frac{u_\phi}{\varepsilon_p r} \frac{\partial u_\phi}{\partial \phi} + \frac{u_z}{\varepsilon_p} \frac{\partial u_\phi}{\partial z} + \frac{u_r u_\phi}{r} \right) = -\frac{1}{r} \frac{\partial p}{\partial \phi} + \frac{\mu}{\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_\phi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_\phi}{\partial \phi^2} + \frac{\partial^2 u_\phi}{\partial z^2} - \frac{u_\phi}{r^2} - \frac{2}{r^2} \frac{\partial u_r}{\partial \phi} \right] + \frac{2\mu}{3\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_\phi}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_\phi}{\partial \phi^2} + \frac{\partial^2 u_\phi}{\partial z^2} - \frac{u_\phi}{r^2} - \frac{2}{r^2} \frac{\partial u_r}{\partial \phi} \right] - \frac{\mu}{K_{br}} u_\phi$$

$$z: \frac{\rho}{\varepsilon_p} \left(\frac{u_r}{\varepsilon_p} \frac{\partial u_z}{\partial r} + \frac{u_\phi}{\varepsilon_p r} \frac{\partial u_z}{\partial \phi} + \frac{u_z}{\varepsilon_p} \frac{\partial u_z}{\partial z} \right) = -\frac{\partial p}{\partial z} + \frac{\mu}{\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_z}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_z}{\partial \phi^2} + \frac{\partial^2 u_z}{\partial z^2} \right] + \frac{2\mu}{3\varepsilon_p} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial u_z}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 u_z}{\partial \phi^2} + \frac{\partial^2 u_z}{\partial z^2} \right] - \frac{\mu}{K_{br}} u_z$$

Continuity equation:

$$\frac{1}{r} \frac{\partial(\rho u_r)}{\partial r} + \frac{1}{r} \frac{\partial(\rho u_\phi)}{\partial \phi} + \frac{\partial(\rho u_z)}{\partial z} = 0$$

G. Appendix G: Fixed Bed Reactor Data

G1: Fixed Bed Experimental Data

Metal species content in condensed sulphuric acid:

Analysis (ICP-AES) was conducted on a sample of sulphuric acid to determine the content of the acid with regard to metal sulphates formed as a result of corrosion and the dominating metal elements found in the acid mixture can be seen in Figure G-1.

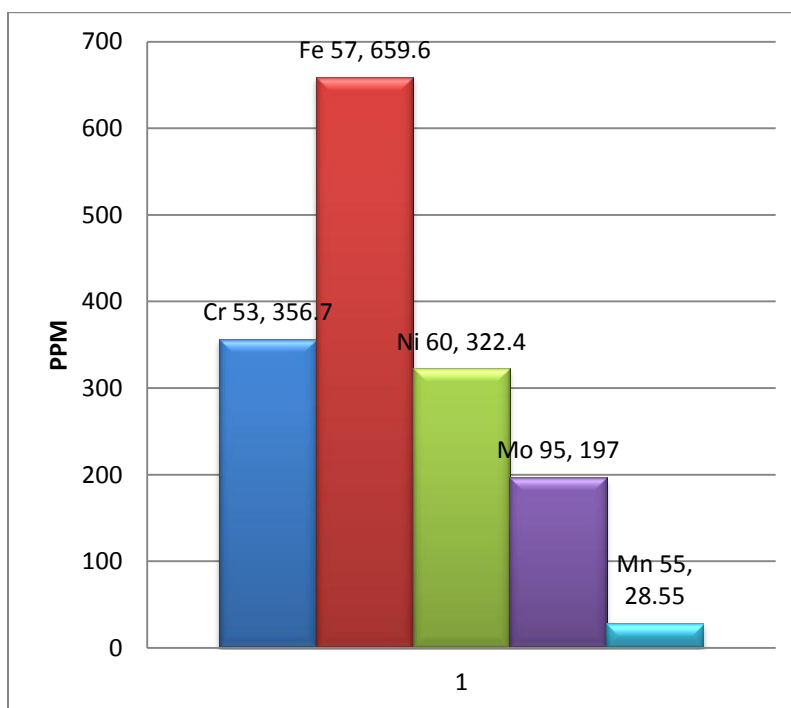


Figure G-1: Metal content in sulphuric acid solution

The high corrosivity of sulphuric acid causes high rate of corrosion in stainless steel by leaching metal ions and forming metal-sulphate combinations. The data in Figure G-1 were found from an acid sample where the whole reactor system was constructed of SS316L. The acid sample collected had a green colour and as found from analysis there was a high concentration of metal ions in the solution. This is just to verify that the amount of acid condensed will not necessarily be 100% of the theoretical amount since the Hastelloy c-276 reactor was also equipped with some stainless steel fittings.

Appendix G: Fixed Bed Reactor Data

G2: Heterogeneous Model Data

G.2.1 Model properties

The values used in the 2D homogeneous and heterogeneous model are given in Table G-1. Due to the large quantity of data collected only one set of model data is given in the table.

Table G-1: Model properties of 2D homo and heterogeneous models

	Fluid			Solid	
Parameter	903	Units	Parameter	903	Units
Concentration					
ε_f	0.36	-	ε_p	0.16	-
ρ_b	1177	kg/m ³	ρ_b	2443	kg/m ³
D_m	3.5x10 ⁻⁵	m ² /s	D_{efs}	4.2x10 ⁻⁶	m ² /s
C_{a0}	3.19	mol/m ³	D_k	9.5x10 ⁻⁶	m ² /s
C_{b0}	0.56	mol/m ³	$D_{eff,m}$	1.43x10 ⁻⁷	m ² /s
C_{c0}	0.28	mol/m ³	τ	1.43	-
C_{i0}	4.19	mol/m ³			
C_{n0}	5.67	mol/m ³			
Thermal					
λ_f	0.055	W/m.K	λ_s	3.5	W/m.K
$\bar{M}_w$	0.0273	kg/mol	$c_{p,s}$	935	J/kg.K
$c_{p,f}$	52	J/mol.K	$T_{s,0}$	903	K

Appendix G: Fixed Bed Reactor Data

T_0	903	K			
P_0	105	kPa			
ε_f	0.36	-			
ρ_f	0.49	kg/m ³			
μ_f	3×10^{-5}	Pa.s			

G.2.2 Supplementary data

Table G-2 provides the error percentage for the average conversion predicted by the advance model versus experimental results obtained.

Table G-2: Error percentages for average conversion by model versus experimental

	Temperature (K)			
Velocity	903	953	1003	1053
1 m/s	14	16	11	10
1.23 m/s	16	11	15	53
1.32 m/s	8	1	12	31

H. Appendix H: Catalyst Characteristics

H1: H₂ Chemisorption:

Sample 1

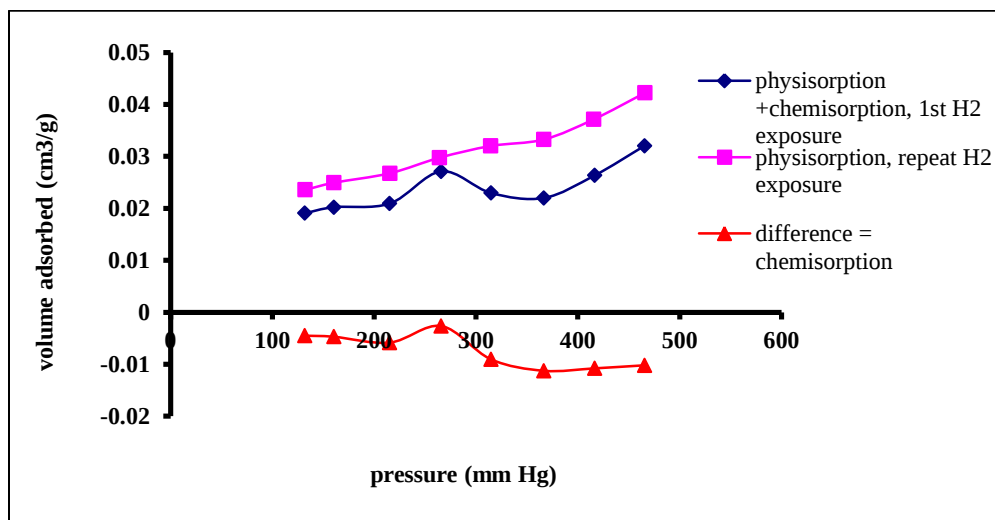


Figure H-1: H₂ Chemisorption – Sample 1

Sample 2:

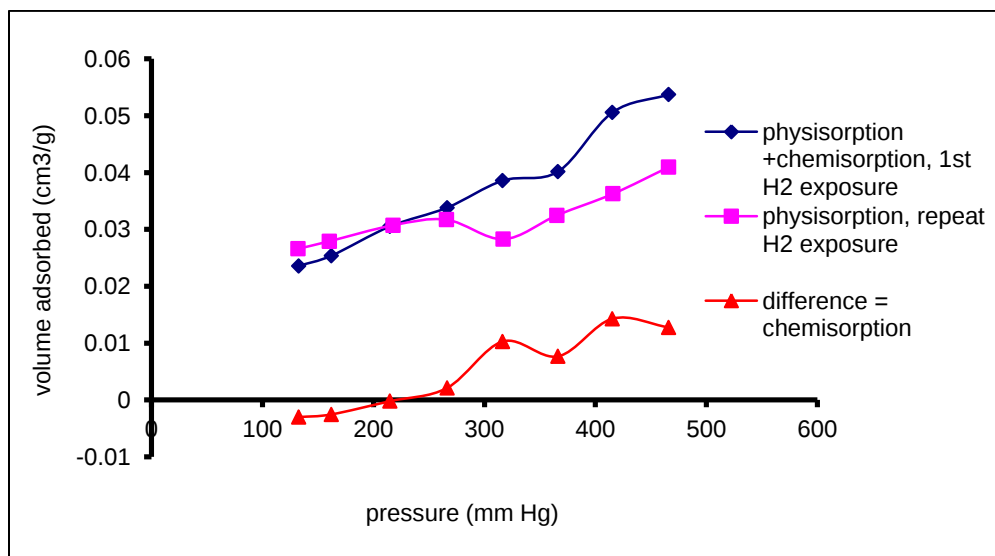


Figure H-2: H₂ Chemisorption – Sample 2

Sample 3:

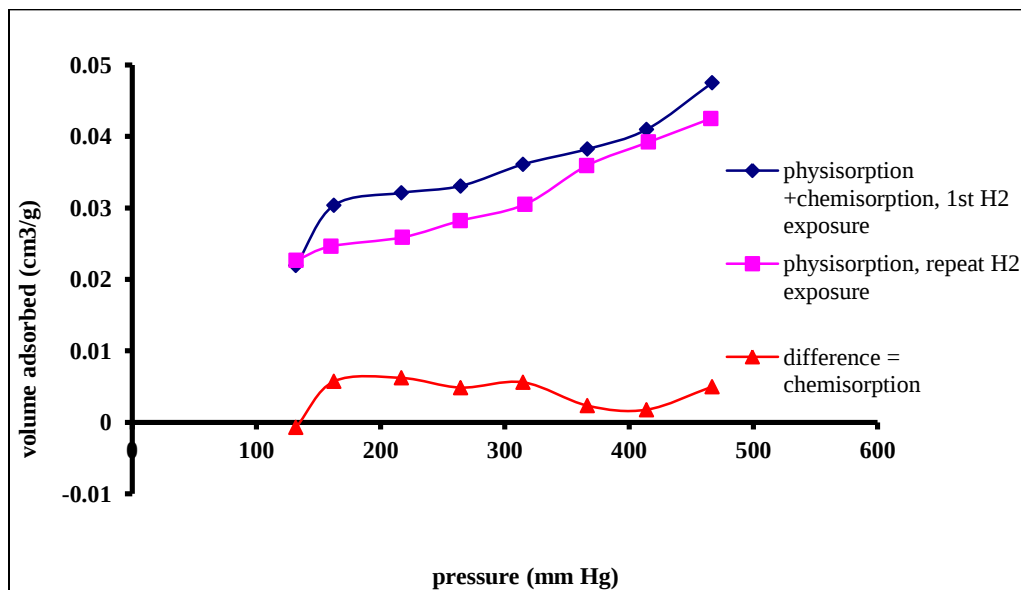


Figure H-3: H₂ Chemisorption – Sample 3

Sample 4:

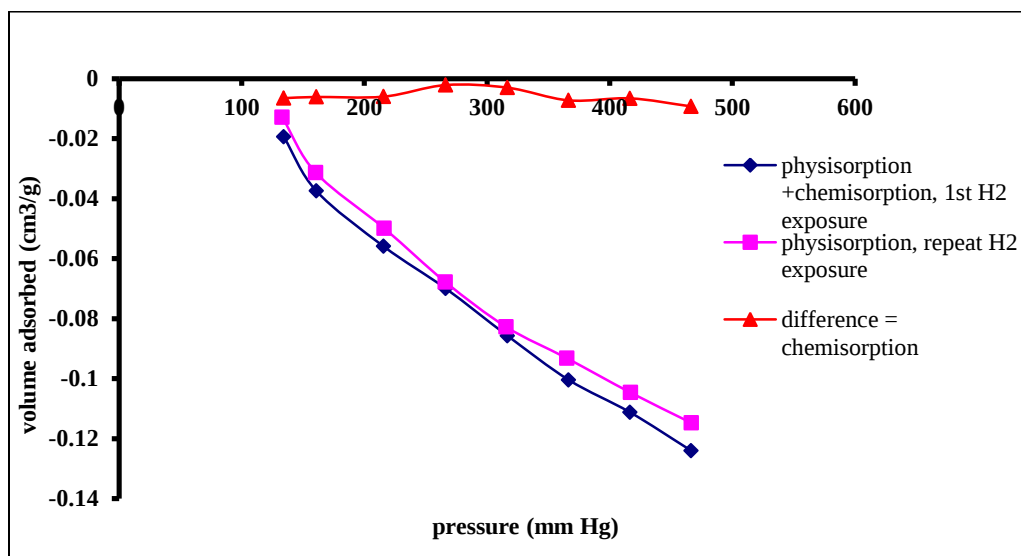


Figure H-4: H₂ Chemisorption – Sample 4

Sample 5:

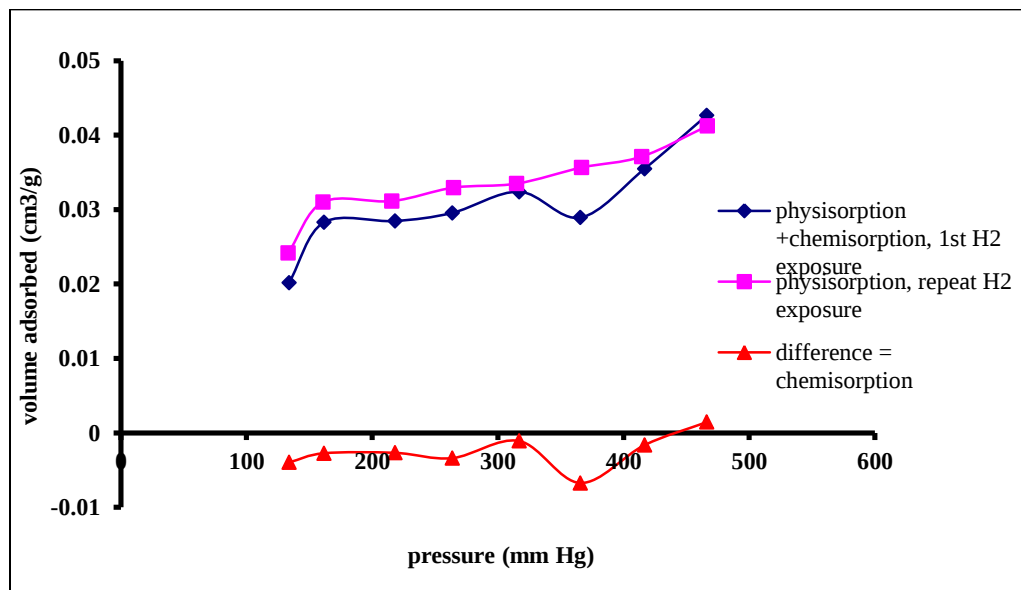


Figure H-5: H₂ Chemisorption – Sample 5

Sample 6:

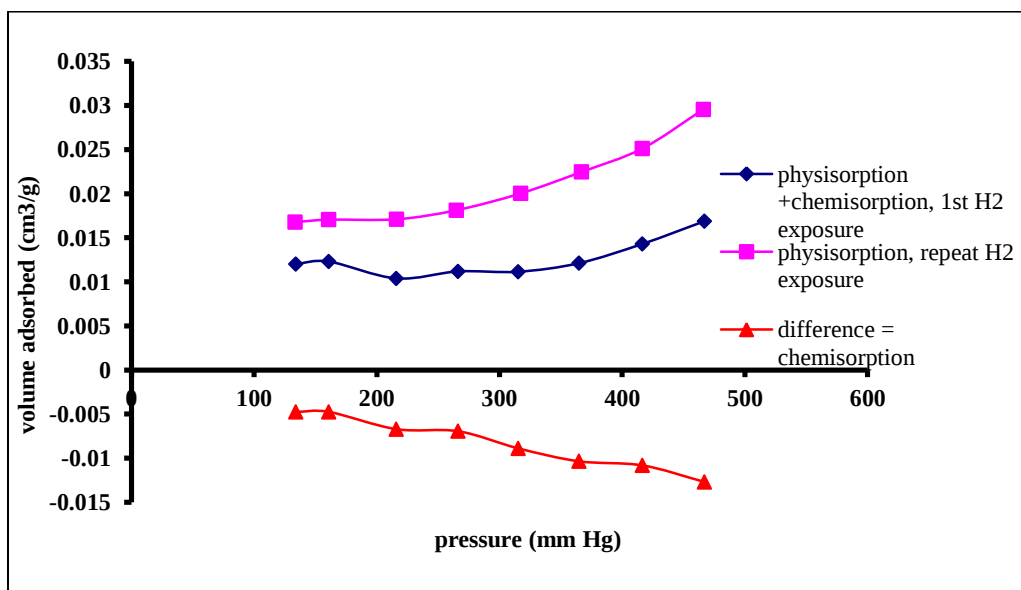


Figure H-6: H₂ Chemisorption – Sample 6

Appendix H: Catalyst Characteristics

Table H-1: H₂ Chemisorption analysis results (Sample numbers indicated)

	1	2	3	4	5	6
Metal Dispersion:	2.6634 %	1.8451 %	2.9850 %	2.3120 %	2.9252 %	1.5623 %
Metallic Surface Area (m ² /g sample):	0.0658	0.0456	0.0737	0.0571	0.0722	0.0386
Metallic Surface Area (m ² /g metal):	6.5782	4.5571	7.3725	5.7103	7.2247	3.8586
Crystallite Size (6.000 V / A) (nm):	42.52223	61.38109	37.94099	48.98497	38.71696	72.49229
Y-Intercept	0.0153 ±	0.0106 ±	0.0171 ±	0.0133 ±	0.0168 ±	0.0090 ±
Quantity Adsorbed (cm ³ /g STP):	0.0027	0.0019	0.0023	0.0045	0.0033	0.0016
Slope:	0.000029 ± 0.000009	0.000090 ± 0.000006	0.000061 ± 0.000007	-0.000303 ± 0.000014	0.000048 ± 0.000011	0.000012 ± 0.000005
Correlation Coefficient:	8.06510E-01	9.86979E-01	9.60302E-01	-9.93311E-01	8.77398E-01	6.96960E-01
Difference Results						
Metal Dispersion:	-0.1300 %	-1.9145 %	0.5910 %	-0.6817 %	-0.8698 %	-0.2054 %
Metallic Surface Area (m ² /g sample):	-0.0032	-0.0473	0.0146	-0.0168	-0.0215	-0.0051
Metallic Surface Area (m ² /g metal):	-0.3210	-4.7284	1.4596	-1.6837	-2.1483	-0.5073
Crystallite Size (6.000 V / A) (nm):	-871.37927	-59.15695	191.64297	-166.13772	-130.20372	-551.38294
Y-Intercept	-0.0007 ±	-0.0110 ±	0.0034 ±	-0.0039 ±	-0.0050 ±	-0.0012 ±
Quantity						

Appendix H: Catalyst Characteristics

Adsorbed (cm ³ /g STP):	0.0020	0.0022	0.0026	0.0023	0.0023	0.0004
Slope:	-0.000023 ± 0.000006	0.000055 ± 0.000007	0.000002 ± 0.000008	-0.000007 ± 0.000007	0.000008 ± 0.000007	-0.000024 ± 0.000001
Correlation Coefficient:	-8.19069E-01	9.53219E-01	7.62321E-02	-3.45515E-01	4.14597E-01	-9.90468E-01

H2: N₂ Physisorption (BET)

Sample 1:

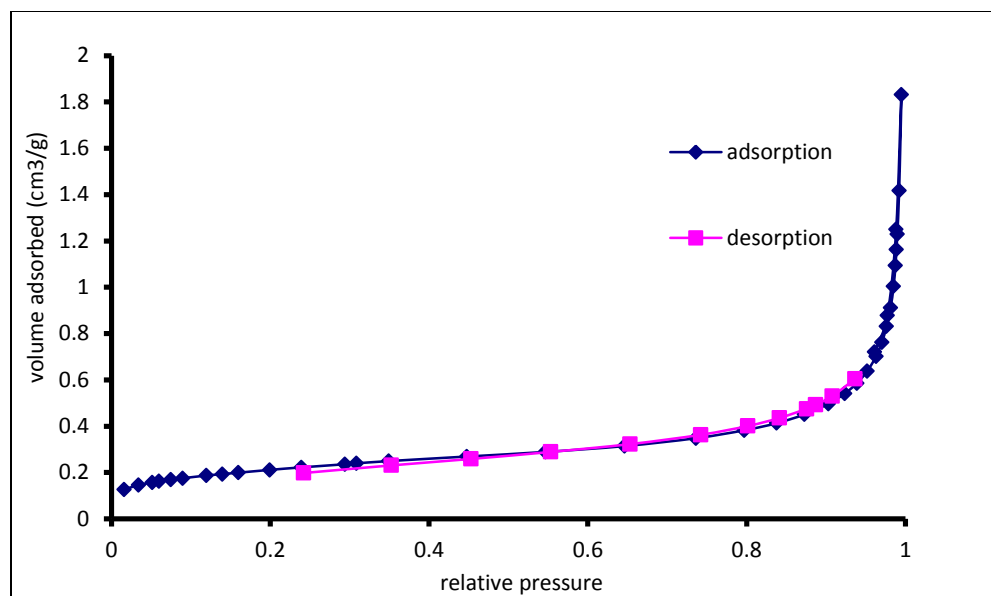


Figure H-7: BET Analysis – Sample 1

Sample 2:

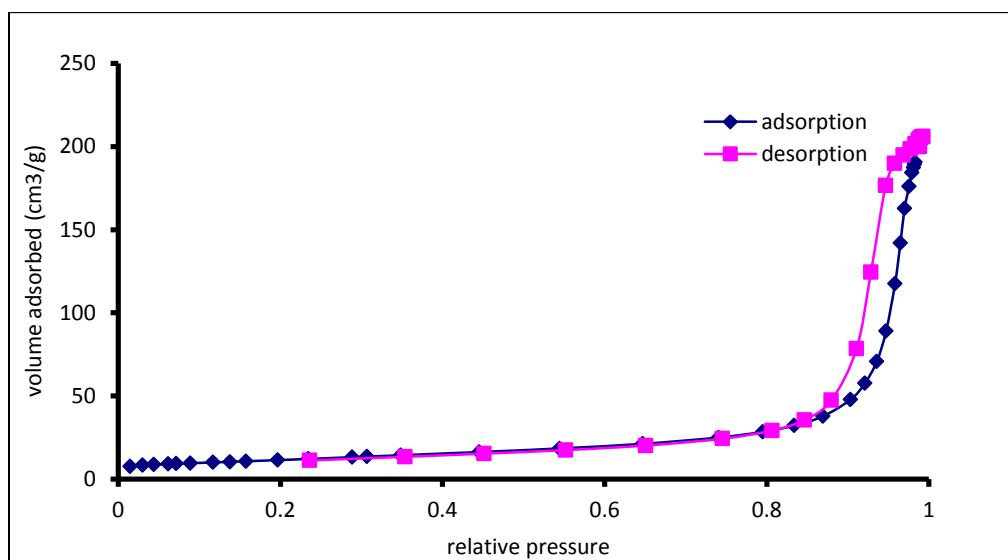


Figure H-8: BET Analysis – Sample 2

Sample 3:

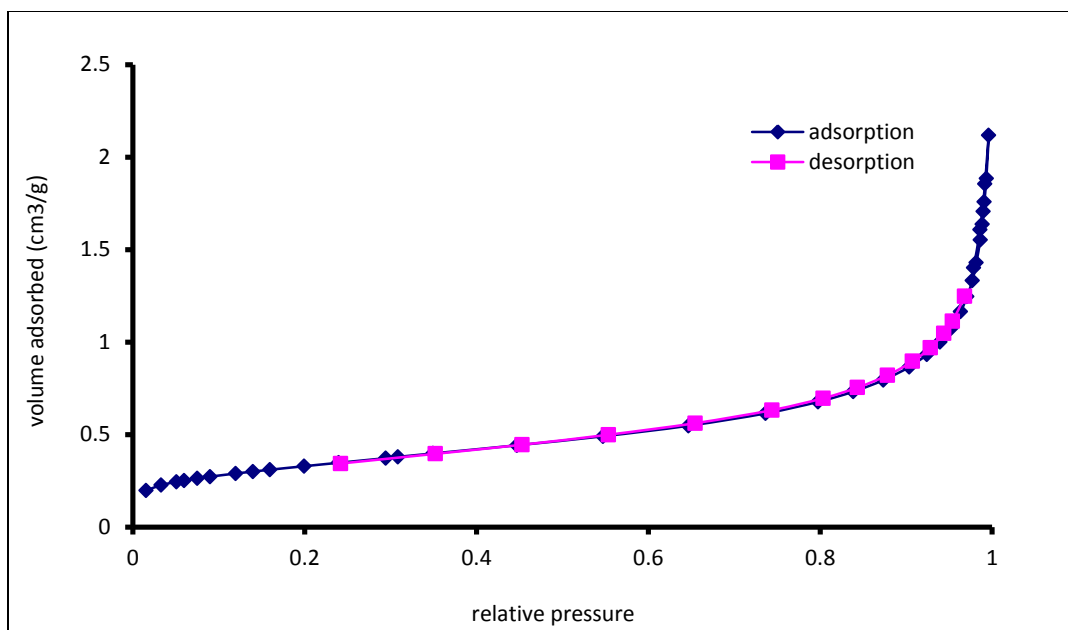


Figure H-9: BET Analysis – Sample 3

Sample 4:

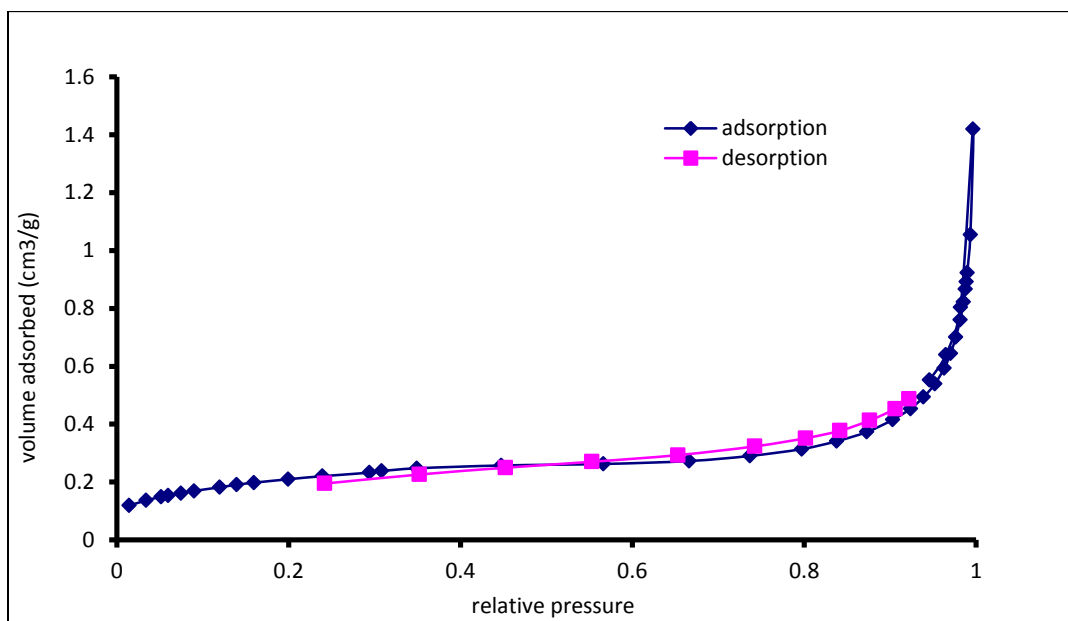


Figure H-10: BET Analysis – Sample 4

Sample 5:

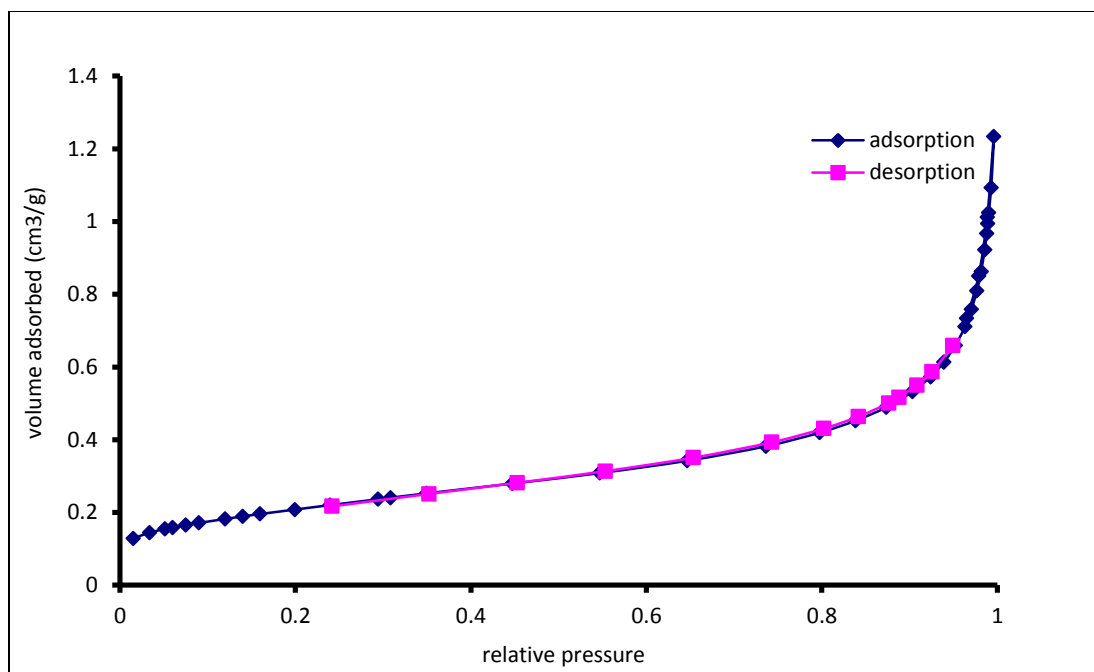


Figure H-11: BET Analysis – Sample 5

Sample 6:

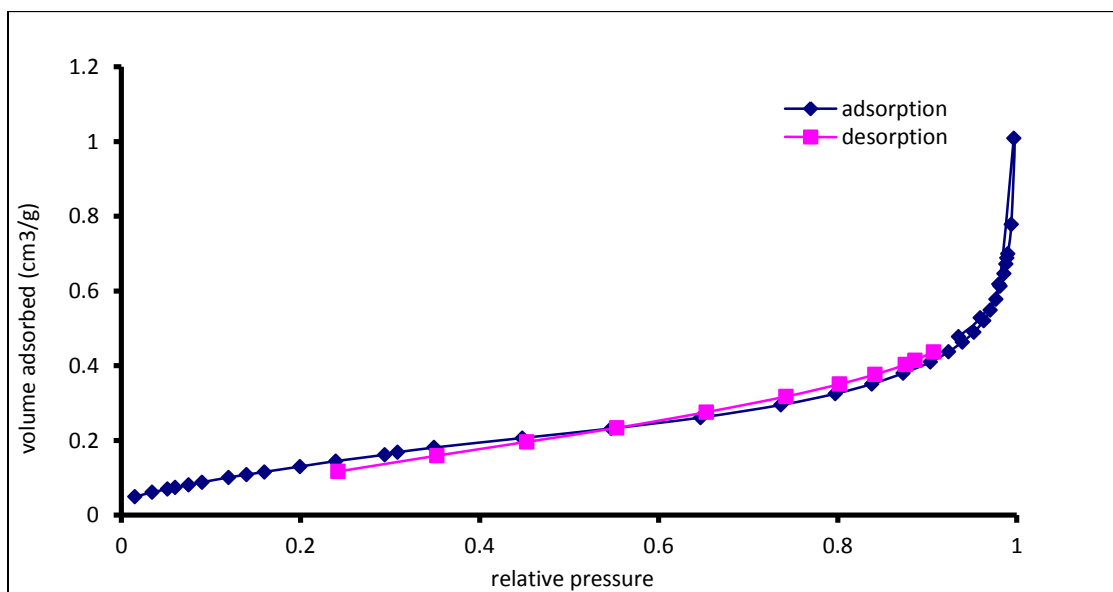


Figure H-12: BET Analysis – Sample 6

H3: TPR Analysis

Sample 1:

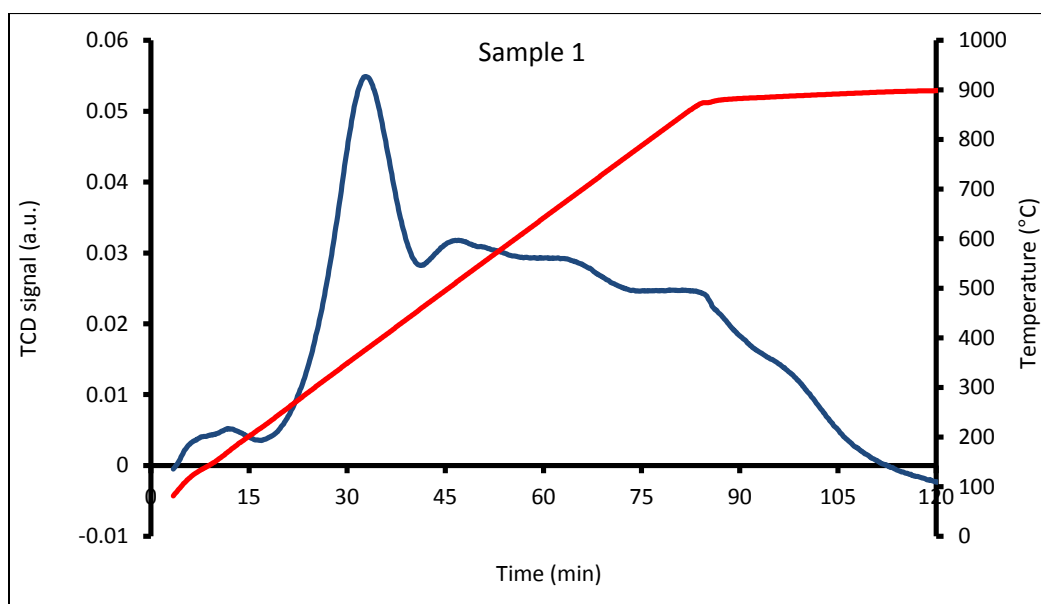


Figure H-13: TPR Analysis – Sample 1

Sample 2:

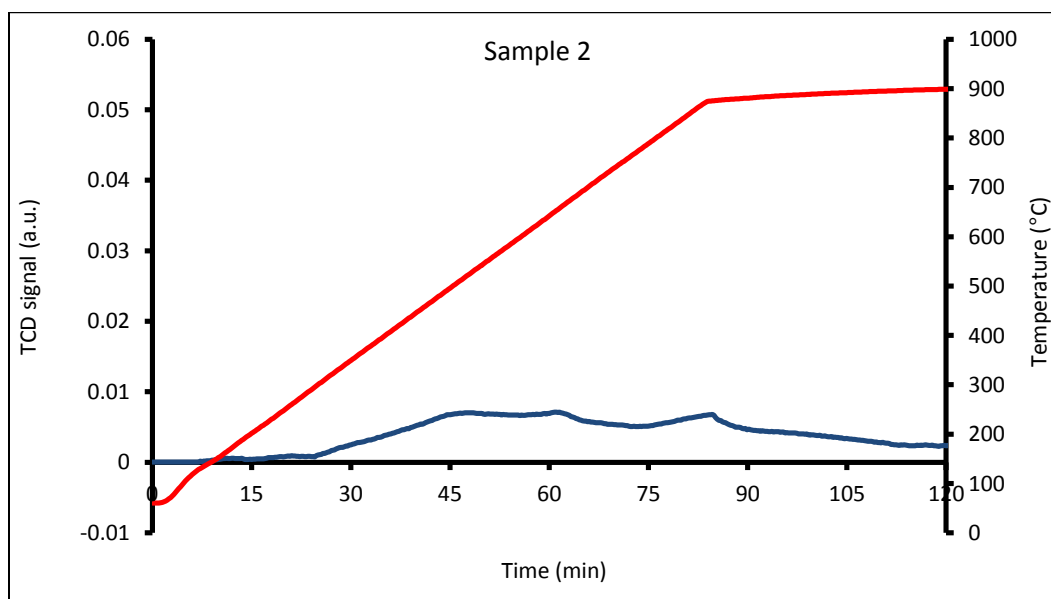


Figure H-14: TPR Analysis – Sample 2

Sample 3:

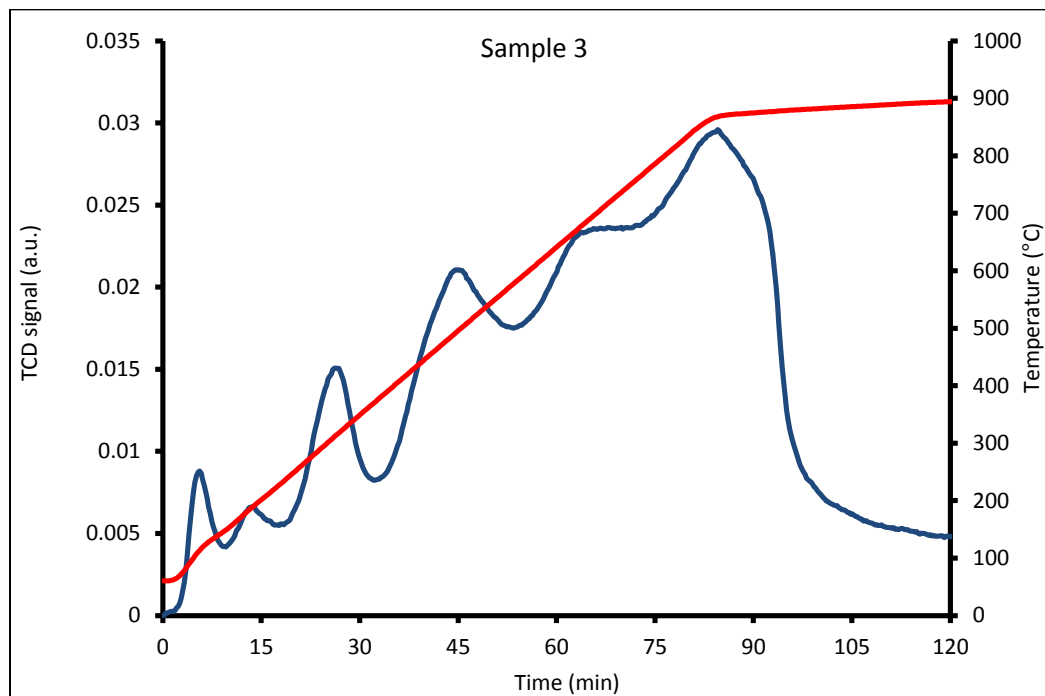


Figure H-15: TPR Analysis – Sample 3

Sample 4:

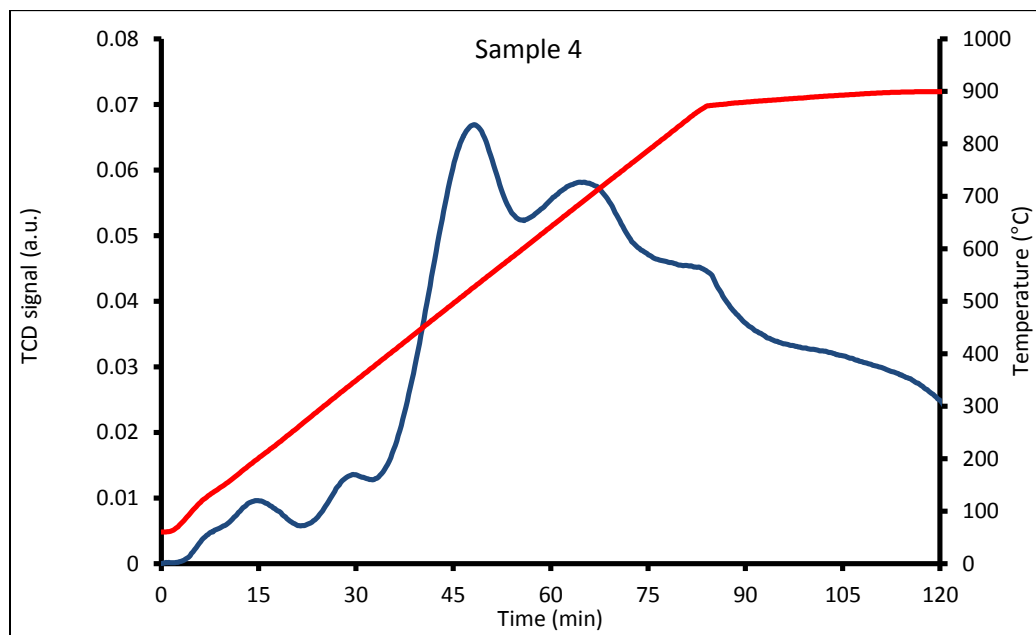


Figure H-16: TPR Analysis – Sample 4

Sample 5:

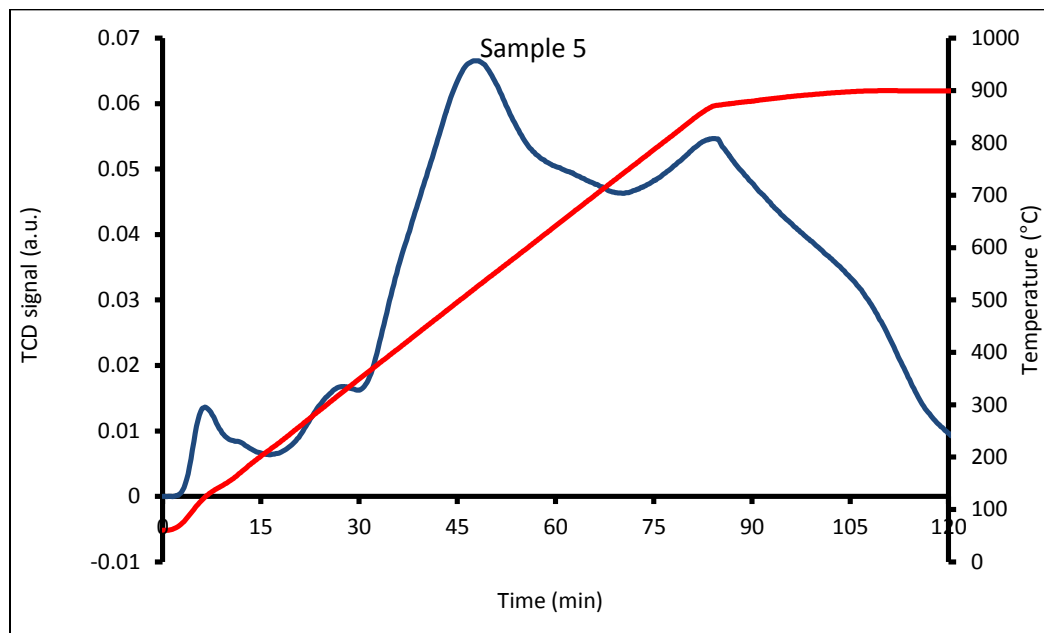


Figure H-17: TPR Analysis – Sample 5

Sample 6:

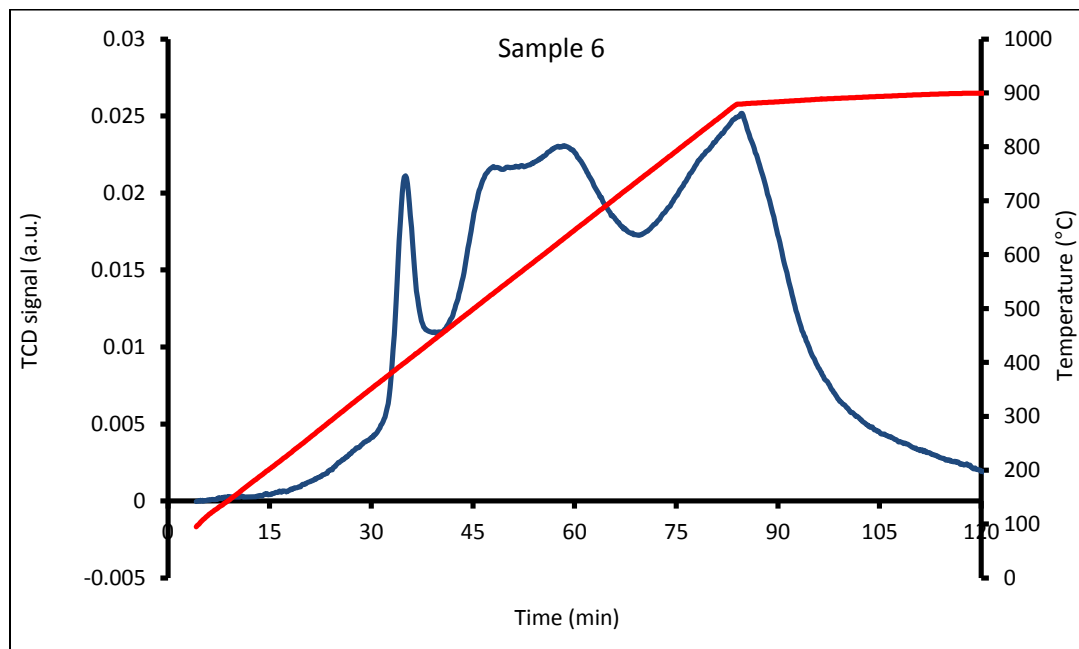


Figure H-18: TPR Analysis – Sample 6

H4: TEM Images

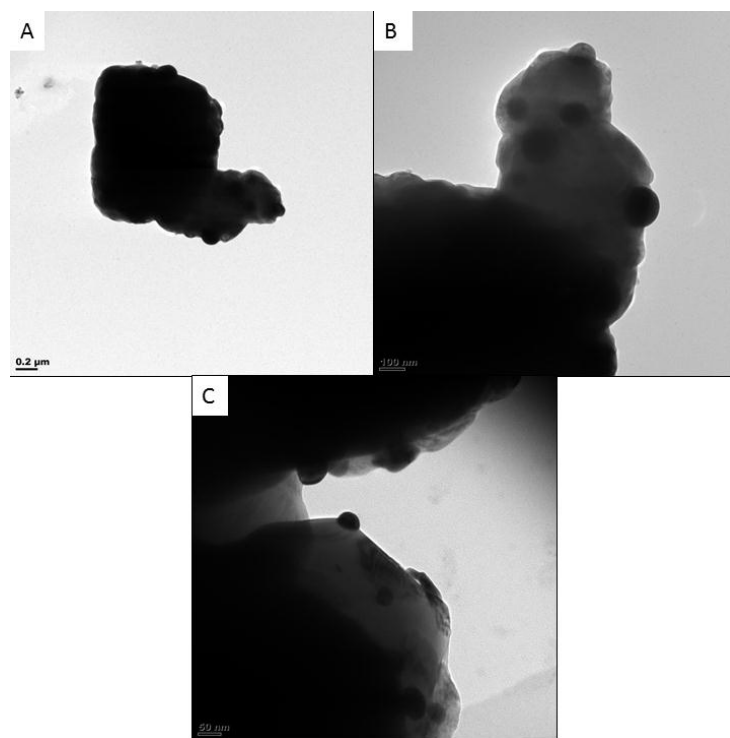


Figure H-19: TEM Images of Sample 1; A: 0.2 μm ; B: 100 nm; C: 50 nm

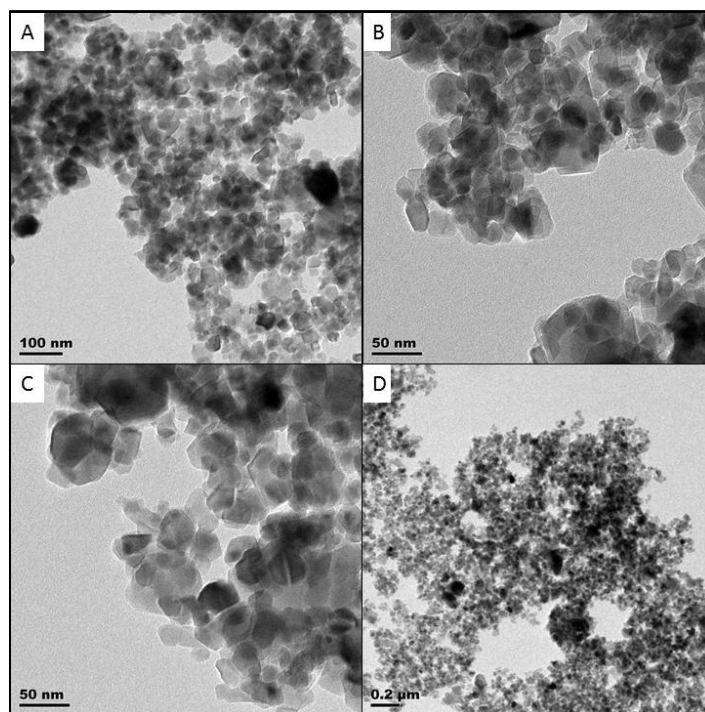


Figure H-20: TEM Images of Sample 2: A: 100 nm; B: 50 nm; C: 50 nm; D: 0.2 μm

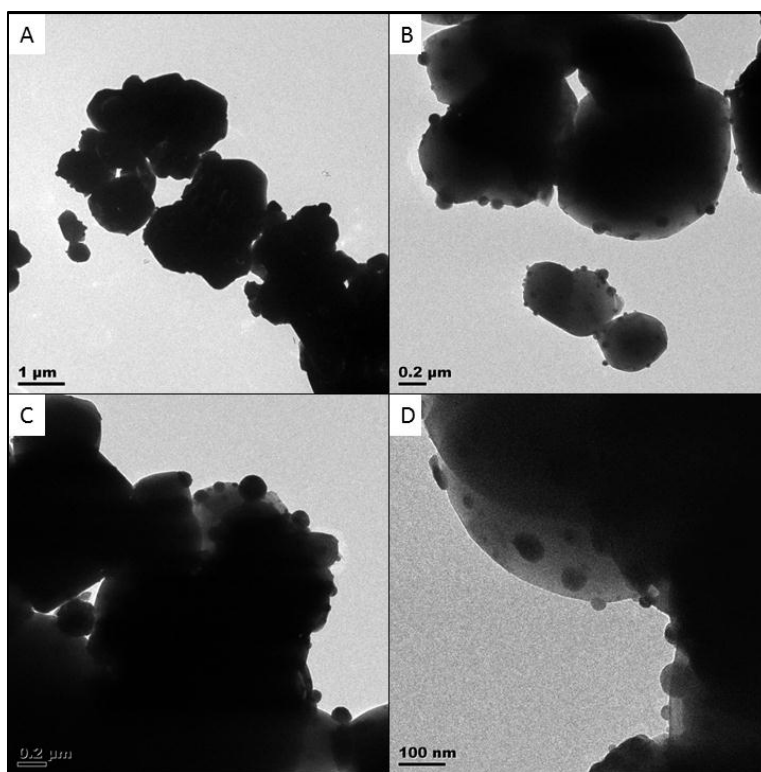


Figure H-21: TEM Images of Sample 3; A: 1 μm ; B: 0.2 μm ; C: 0.2 μm ; D: 100 nm

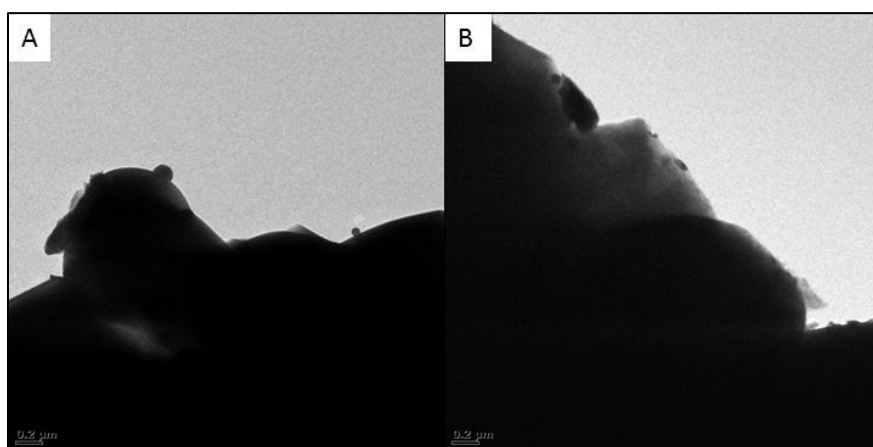


Figure H-22: TEM Images of Sample 4; A: 0.2 μm ; B: 0.2 μm

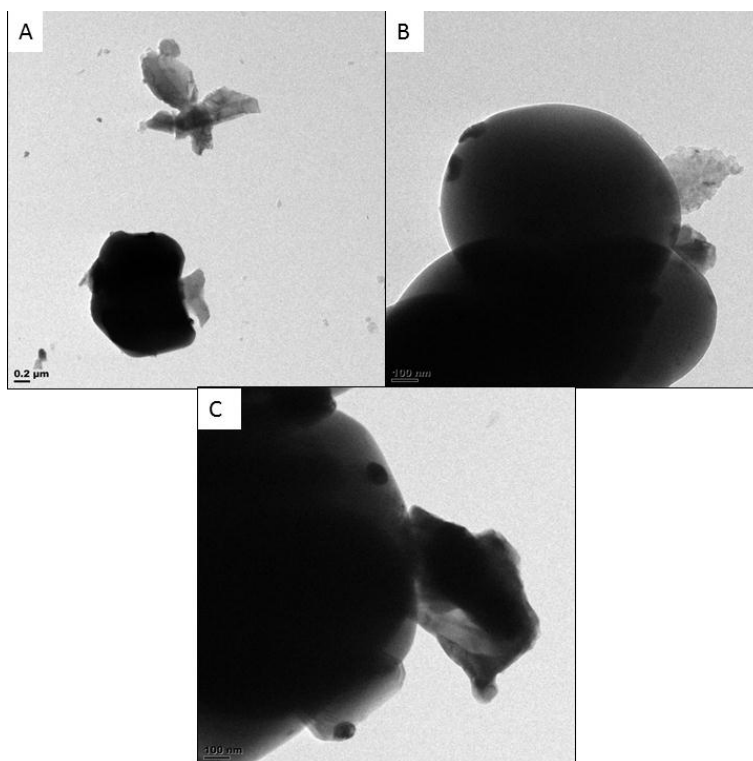


Figure H-23: TEM Images of Sample 5; A: 0.2 μm ; B: 100 nm; C: 100 nm

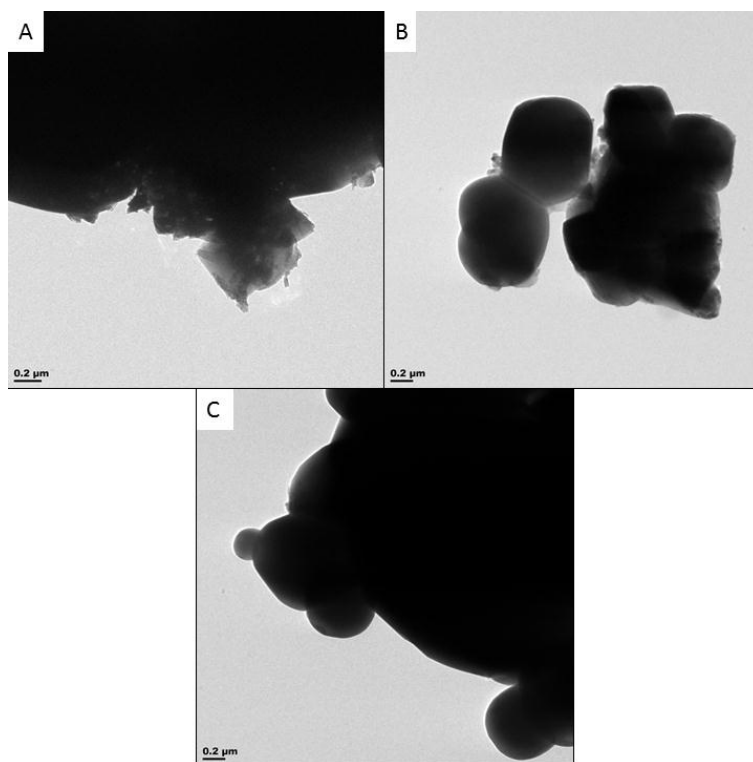


Figure H-24: TEM Images of Sample 6; A: 0.2 μm ; B: 0.2 μm ; C: 0.2 μm

H5: XRD Results

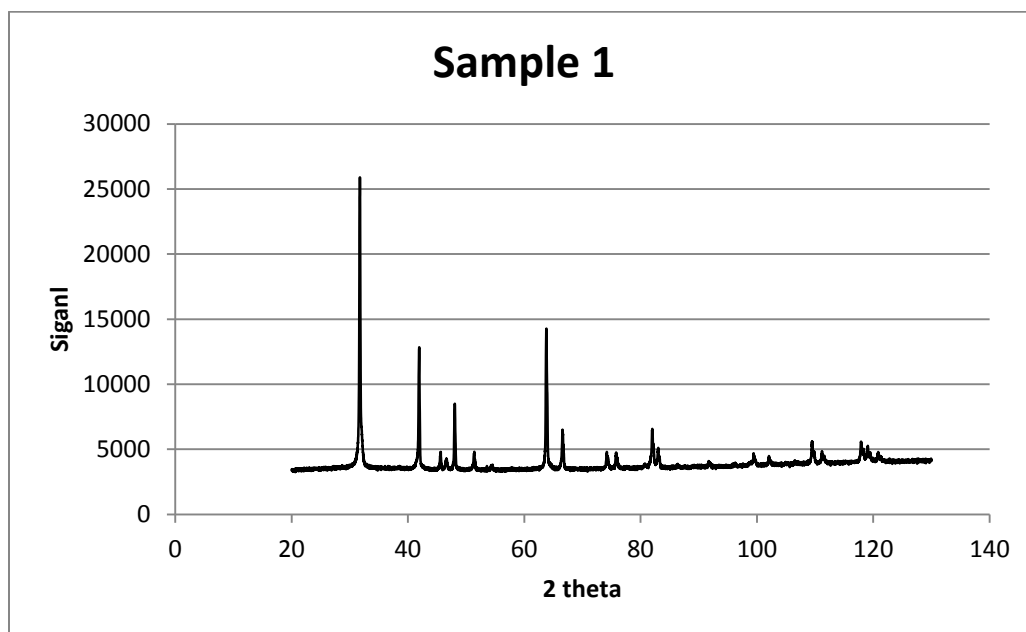


Figure H-25: X-Ray Diffraction Spectrum Sample 1

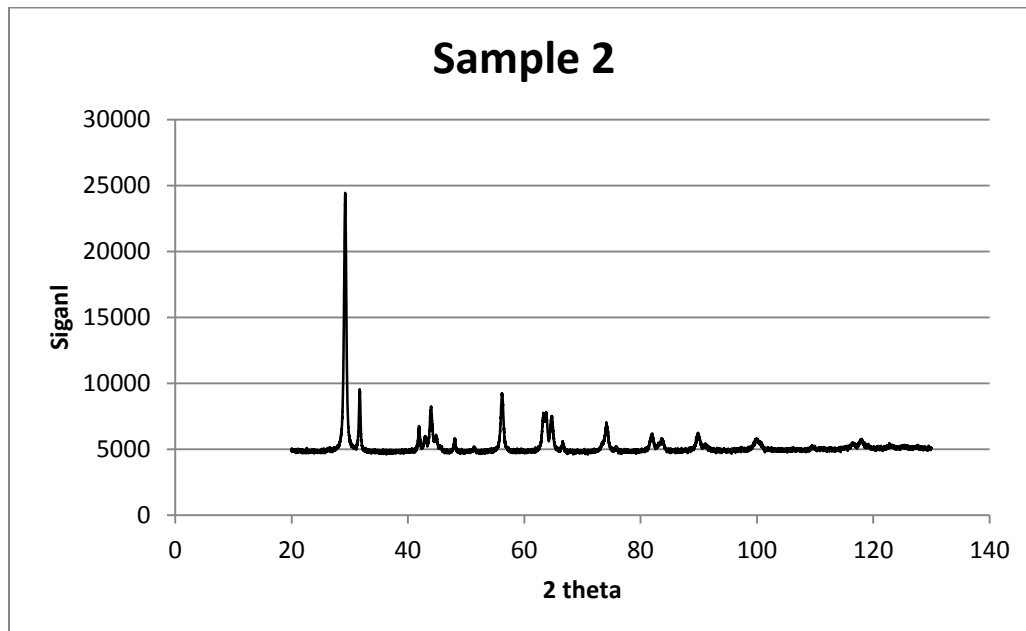


Figure H-26: X-Ray Diffraction Spectrum Sample 2

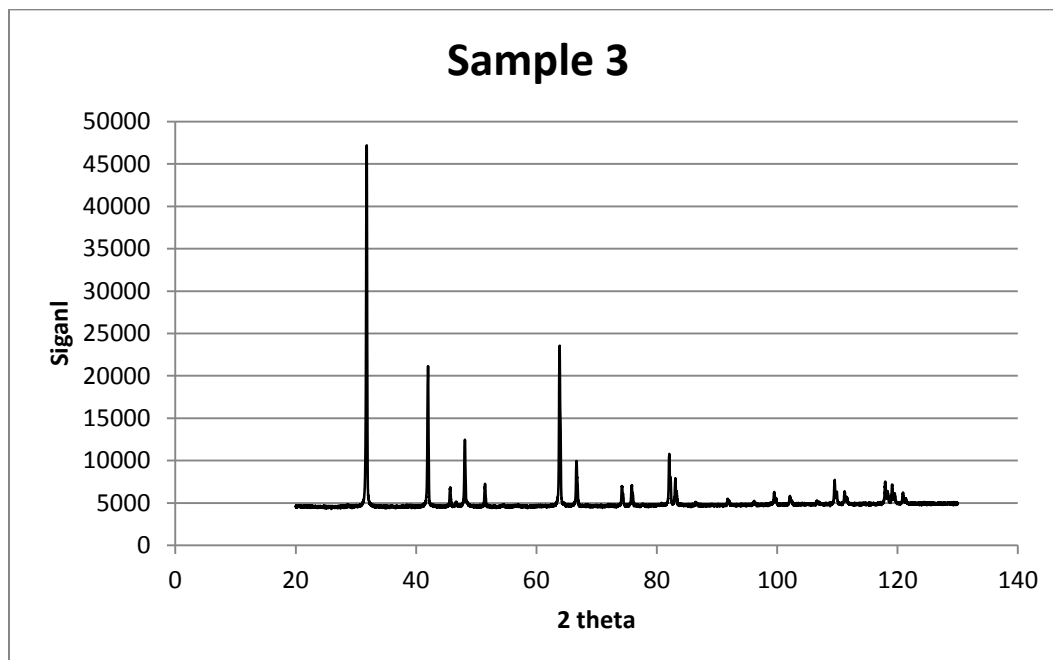


Figure H-27: X-Ray Diffraction Spectrum Sample 3

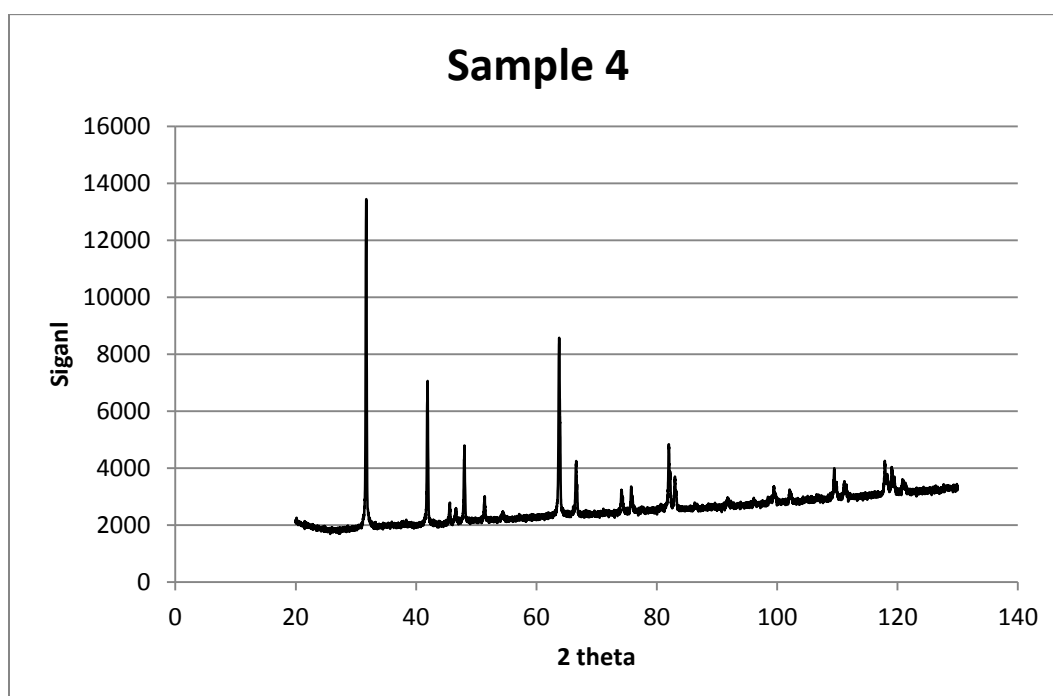


Figure H-28: X-Ray Diffraction Spectrum Sample 4

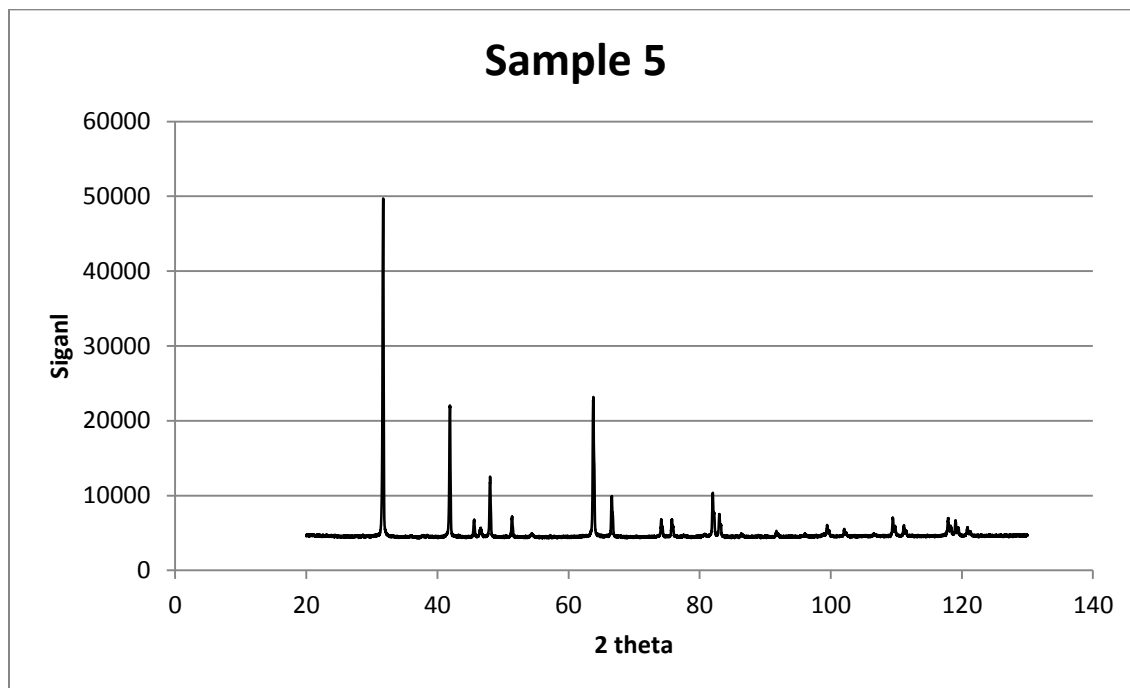


Figure H-29: X-Ray Diffraction Spectrum Sample 5

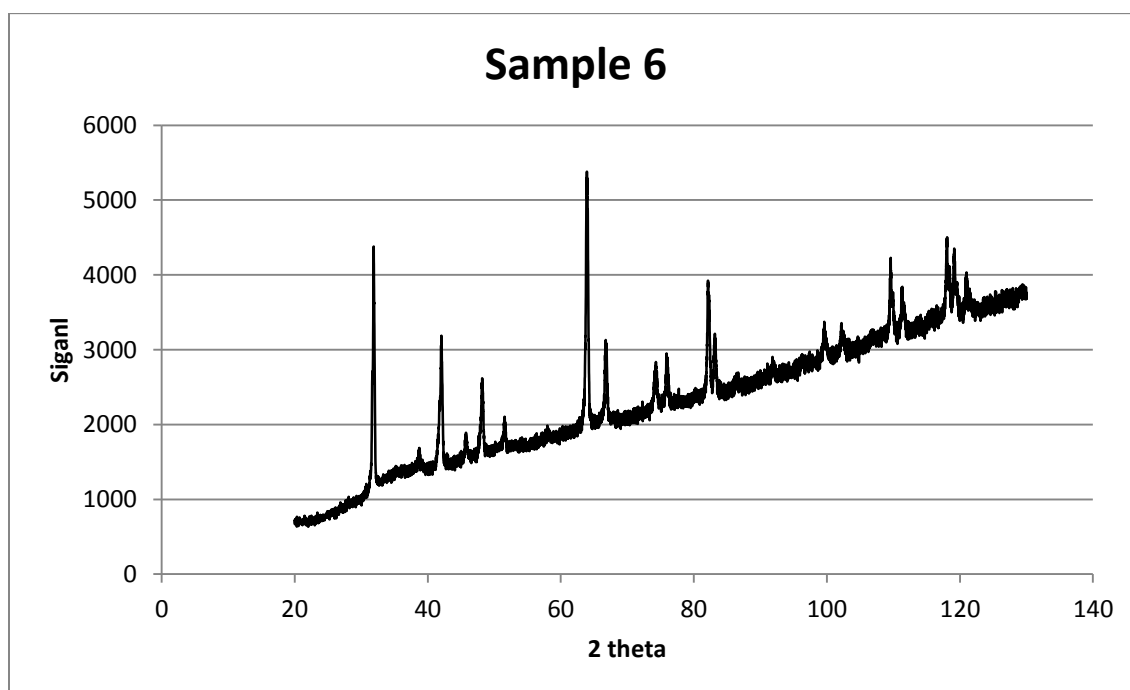


Figure H-30: X-Ray Diffraction Spectrum Sample 6